



KU LEUVEN



Safety evaluation of road infrastructures through unconventional dynamic monitoring and Operational Modal Analysis (OMA) methodologies

***Prestressed Concrete Beams with Artificially Damaged
Strands: Plan of Experimental Tests and Numerical Modeling***

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12 gennaio 2026

Application of OMA Techniques in Python

Application of OMA: Implementing OMA techniques like EFDD, SSI-COV, SSI-DATA, and PolyMax to analyze structural dynamics in response in a new python library (Modalyzer)

```
print('Please upload the EFDD_func.py ...')
# files.upload()
# importlib.reload(EFDD_func) # Reload the module
from EFDD_func import FDD_SVD_Diagram, FDD_ModeShape, FDD_Damping, MAC_Calculation

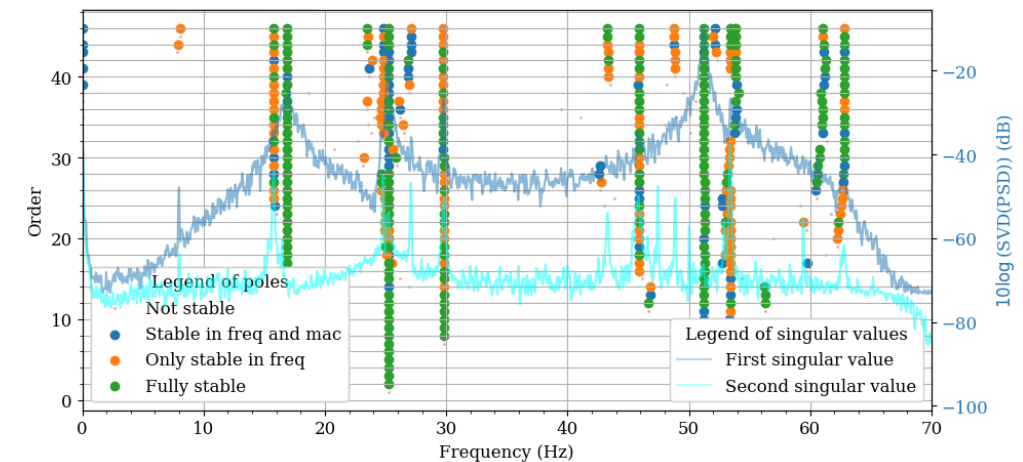
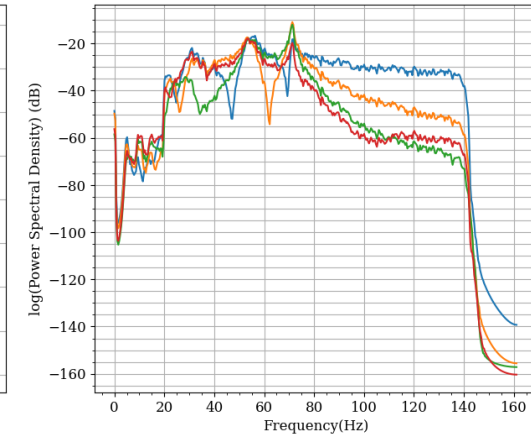
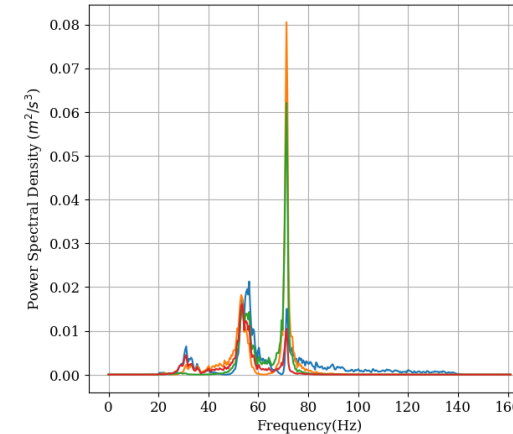
print('upload SSI_func.py ...')
# files.upload()
from SSI_func import SSI_Alg, psd_func, svd_psd, stabilization_diagram

print('upload PolyMAX_func.py ...')
# files.upload()
from PolyMAX_func import PolyMAX, independent_mode_shape

print('Please upload the ITD_func.py ...')
# files.upload()
from ITD_func import ITD_alg

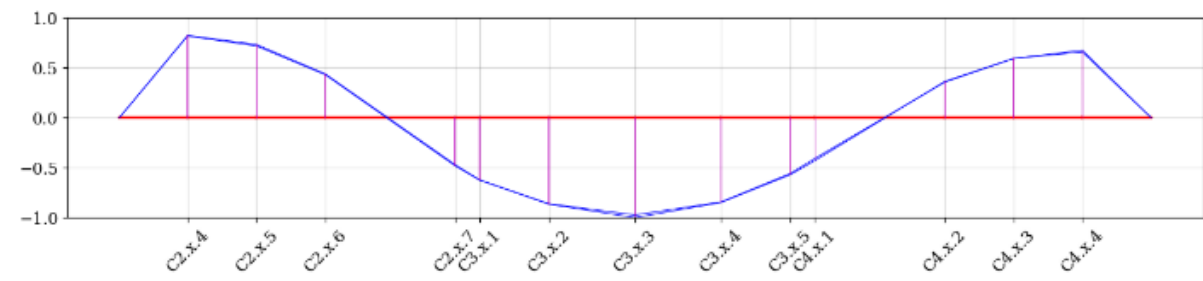
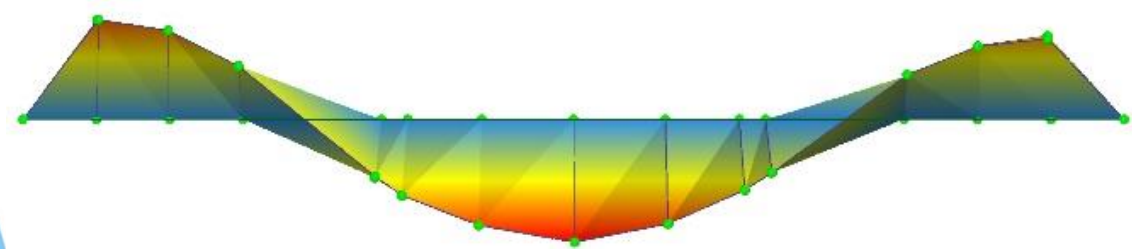
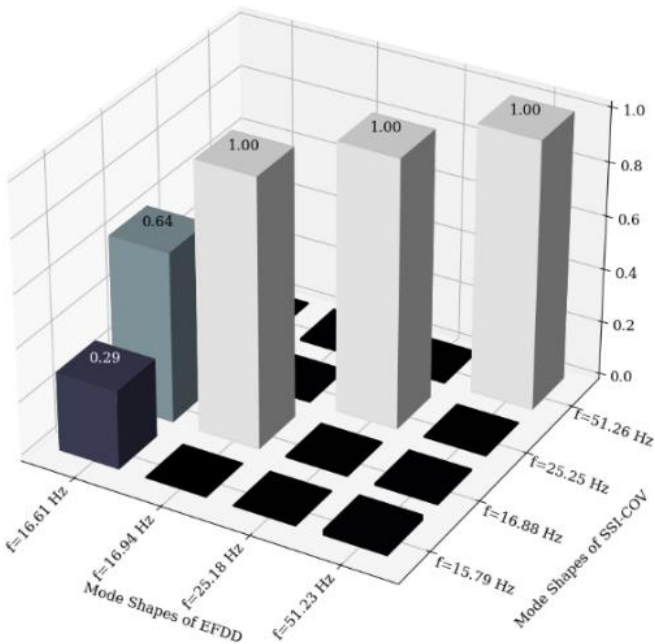
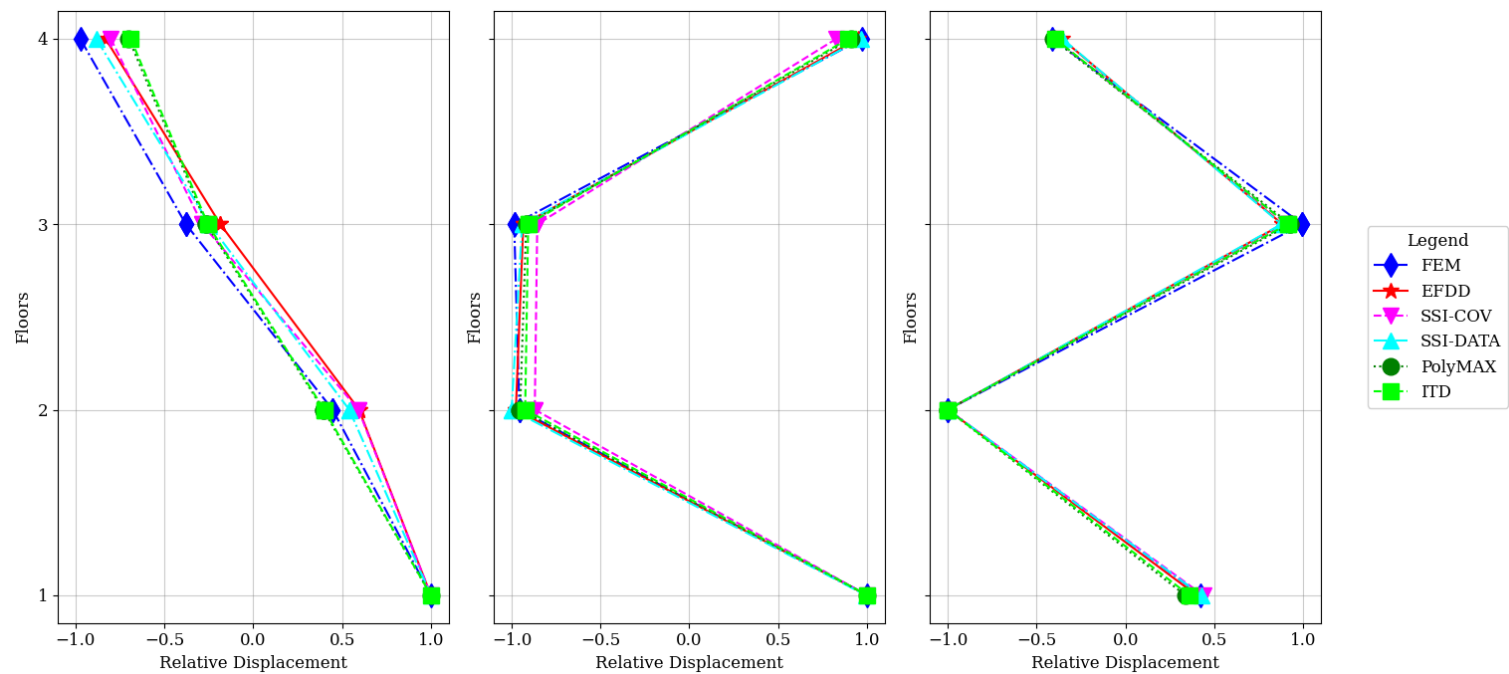
from Preprocess import preprocess, results_table, choose_modes
from ModeShape import draw_mode_shapes, draw_MAC_diagram
```

✓ 0.0s



Application of OMA Techniques in Python

Application of OMA: Mode shapes and MAC matrix



Experimental campaign

1. OBJECTIVES

- Investigate structural health monitoring techniques for prestressed concrete bridge girders.
- Perform experimental testing on artificially damaged strands in a controlled lab environment.
- Use advanced sensors and acquisition units provided by SACERTIS to validate results.

"These objectives aim to advance the understanding of structural damage detection through dynamic monitoring."

2. CONSTRAINTS

Lab Constraints:

- Actuator Sizes: 250 kN, 500 kN, and 1000 kN.
- Control Modes: Displacement-controlled or force-controlled.
- Testing Area Dimensions: 9.0 m x 7.0 m, height 5.0 m.

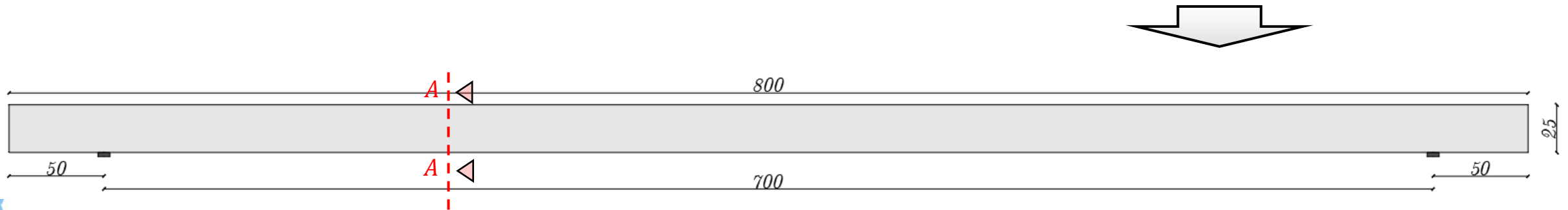
"These constraints define the boundaries of the experimental campaign and influence the design of test setups."



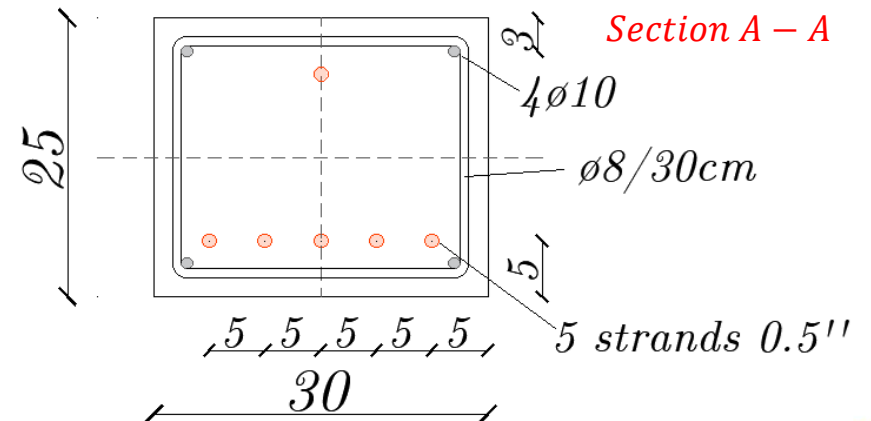
DESIGN OF PRESTRESSED CONCRETE BEAM

Cross section geometry: 30 cm x 25 cm

Length = ? $\Rightarrow$ 8.0 m $\Rightarrow$ 12 prototypes of 8.0 m each (96.0 m of the 100.0 m casting slot), clear span $L = 7.0$ m



Reinforcement = ? $\Rightarrow$ 5+1 prestressing strands 0.5",
area $A_t = 93 \text{ mm}^2$ each

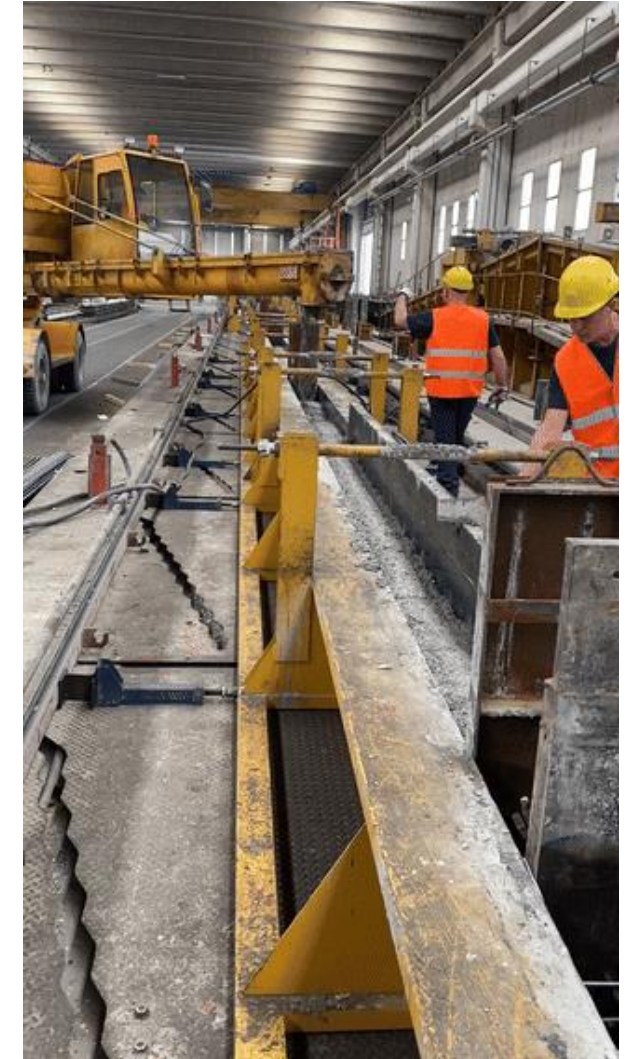
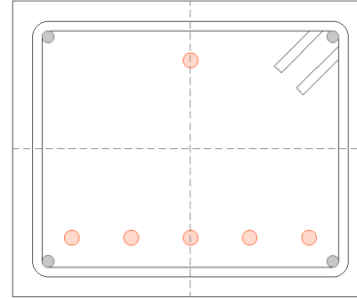


Beam Design and Manufacturer Constraints

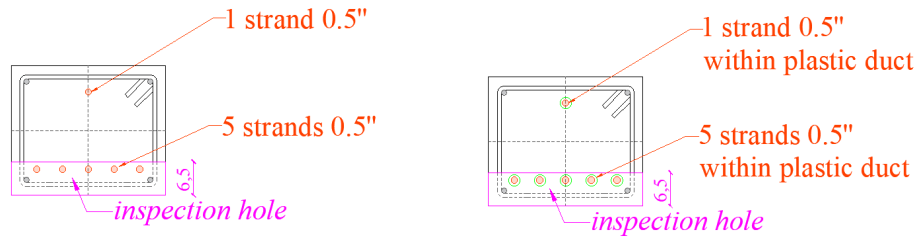
- prestressing strands spacing 5.0 cm in both vertical and horizontal direction
- minimum diameter for prestressing reinforcement $\frac{1}{2}$ " ($A_t = 93 \text{ mm}^2$)
- recommended concrete class C45/55 ($R_{ck} = 55 \text{ MPa}$)
- recommended size of concrete section 30 x 25 cm to exploit ongoing casting setup
- recommended length of total casting 100.0 m
- strands release: approx. 16 hours from casting, when cubic mean strength is at least 35 MPa



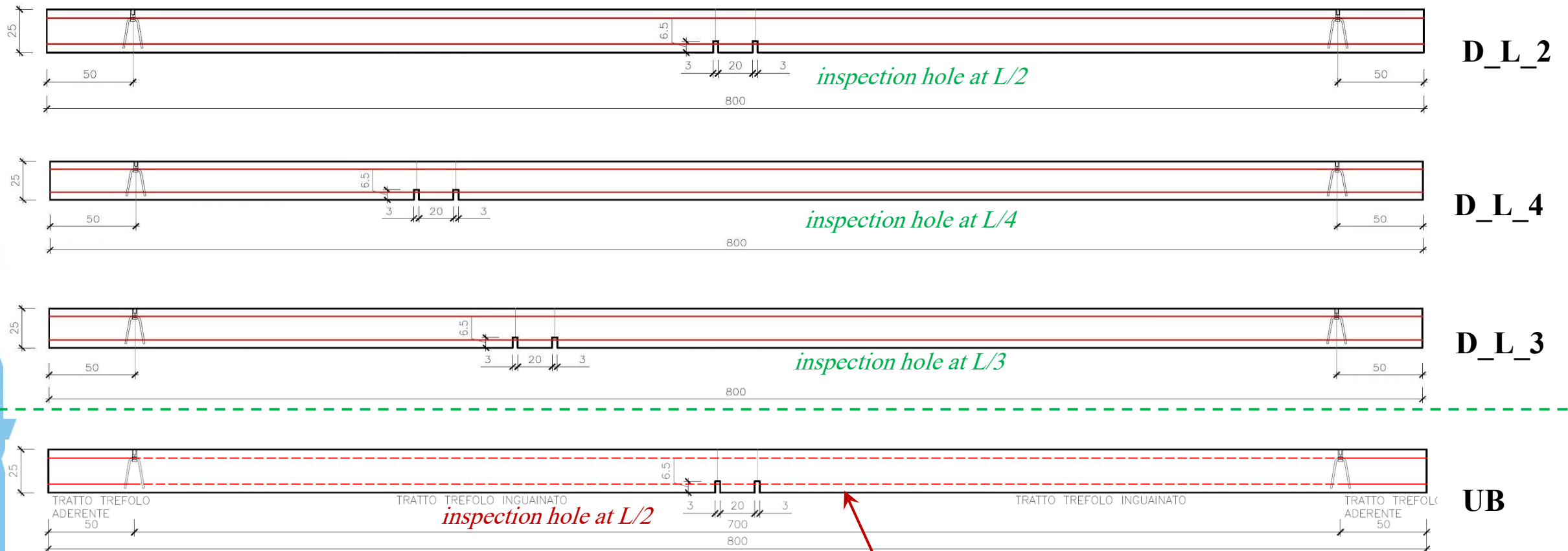
Casting of the specimens



Types of specimens



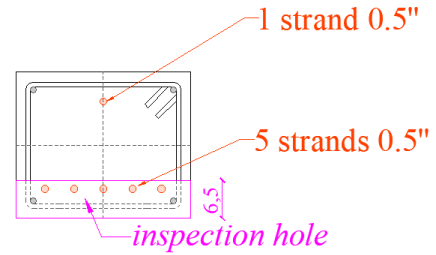
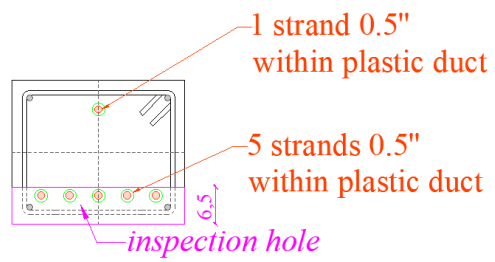
Bonded strands



unbonded strands

12 BEAMS: 9 BONDED 3 UNBONDED

Types of specimens

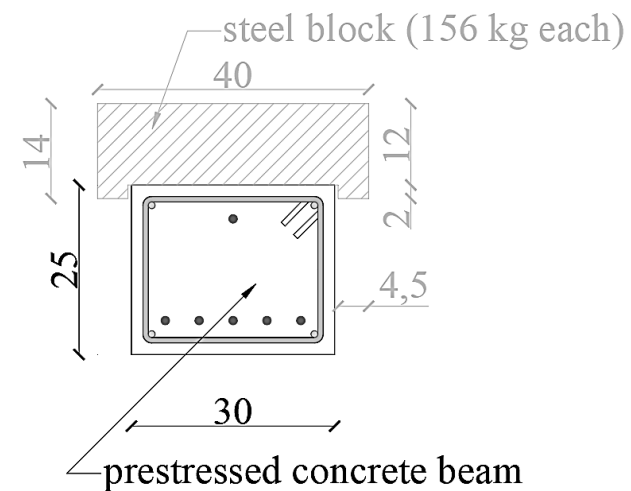
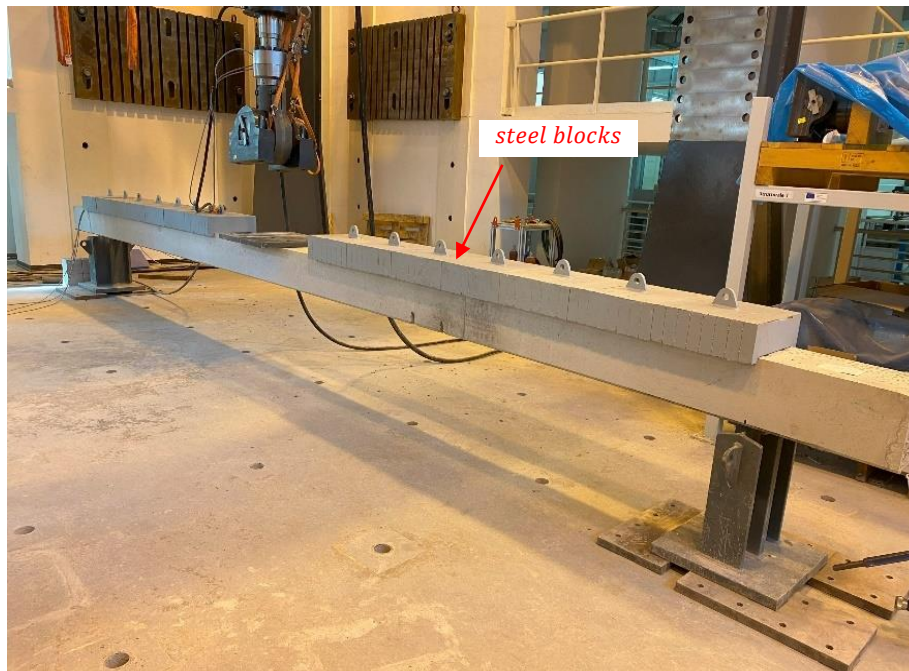
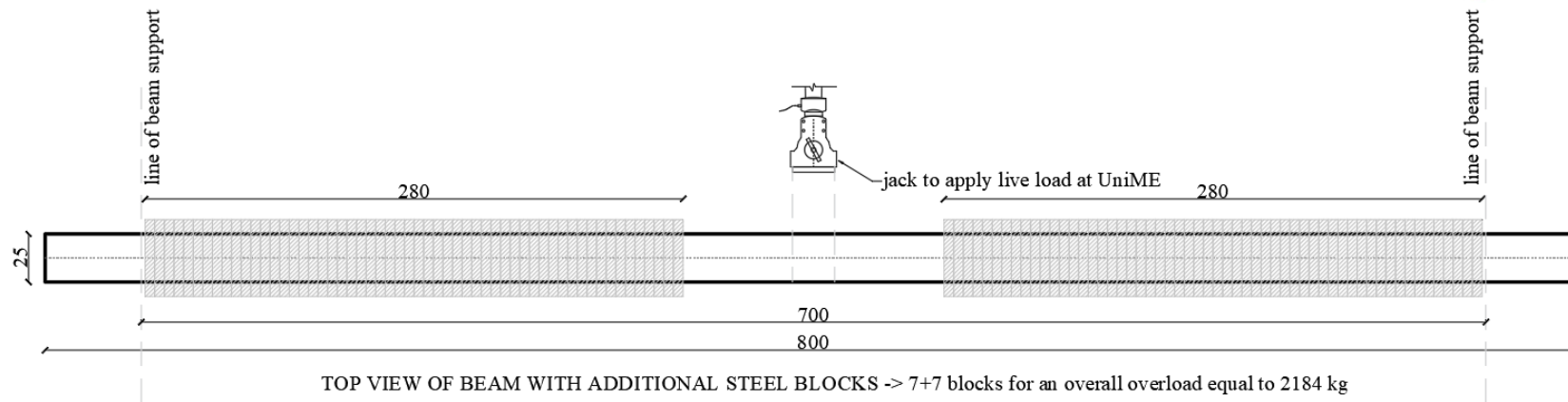


unbonded strands

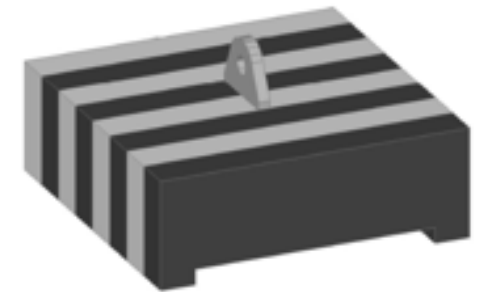


Bonded strands

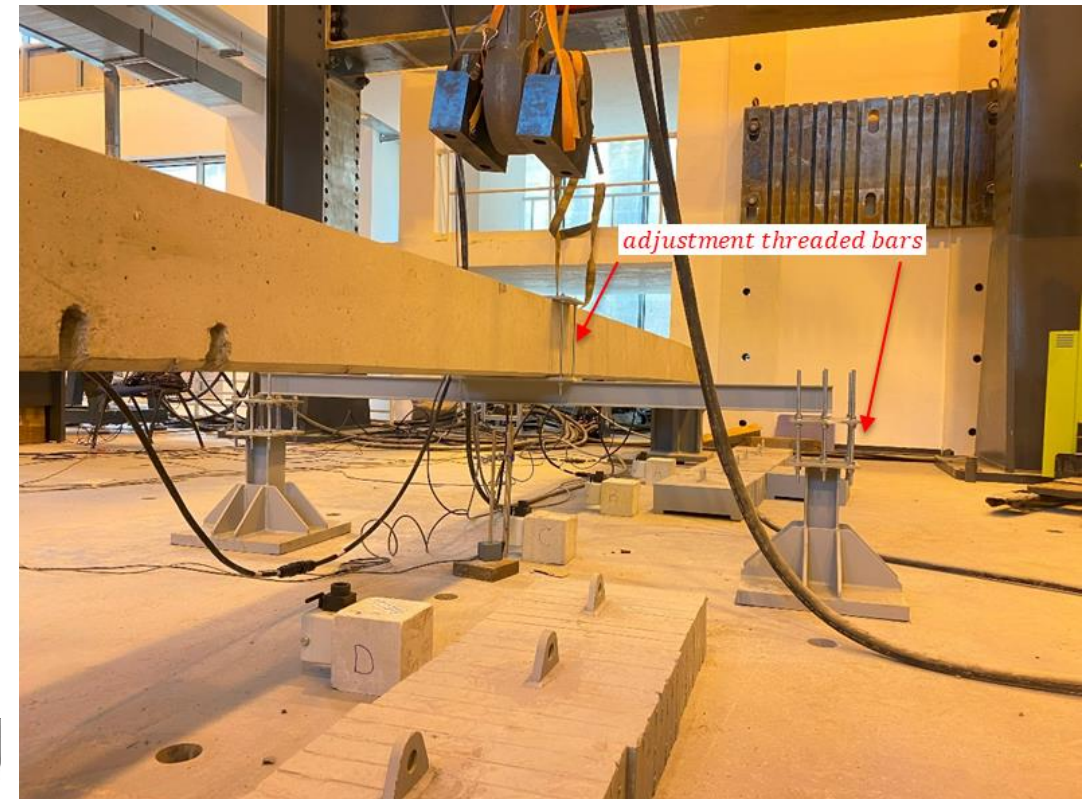
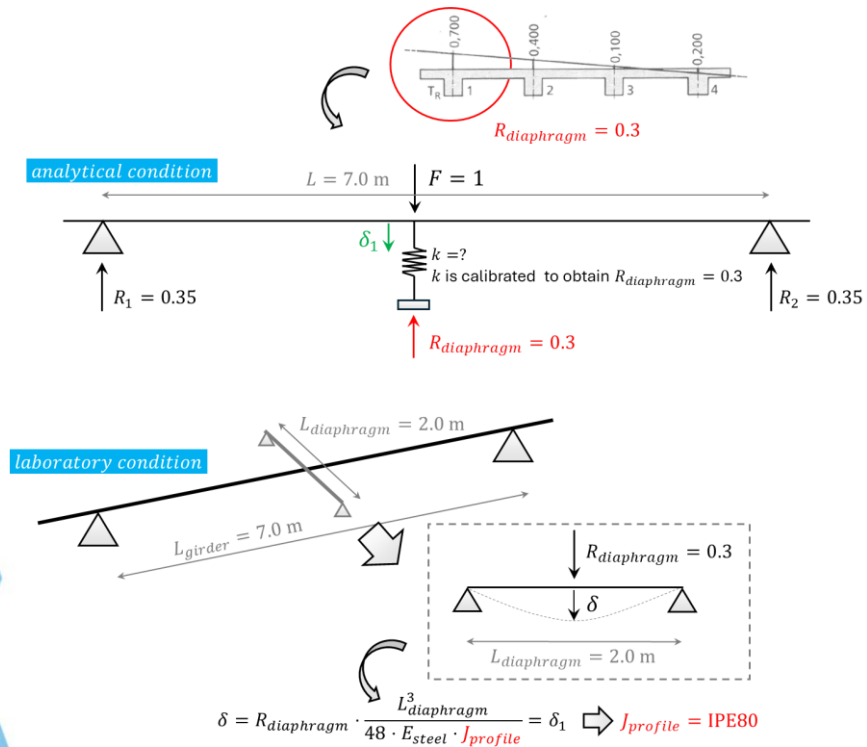
OVERLOAD WITH ADDED STEEL BLOCKS ON THE BEAM



steel block 156 kg each

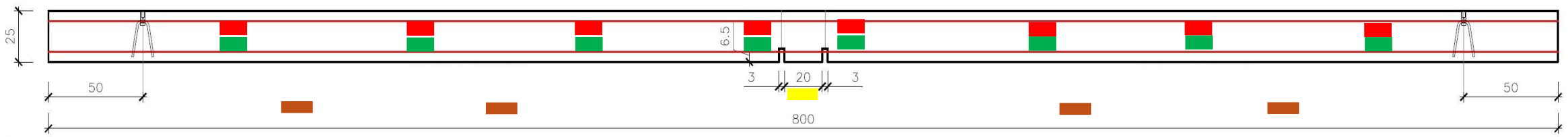


Simulation of the effect of transverse diaphragms



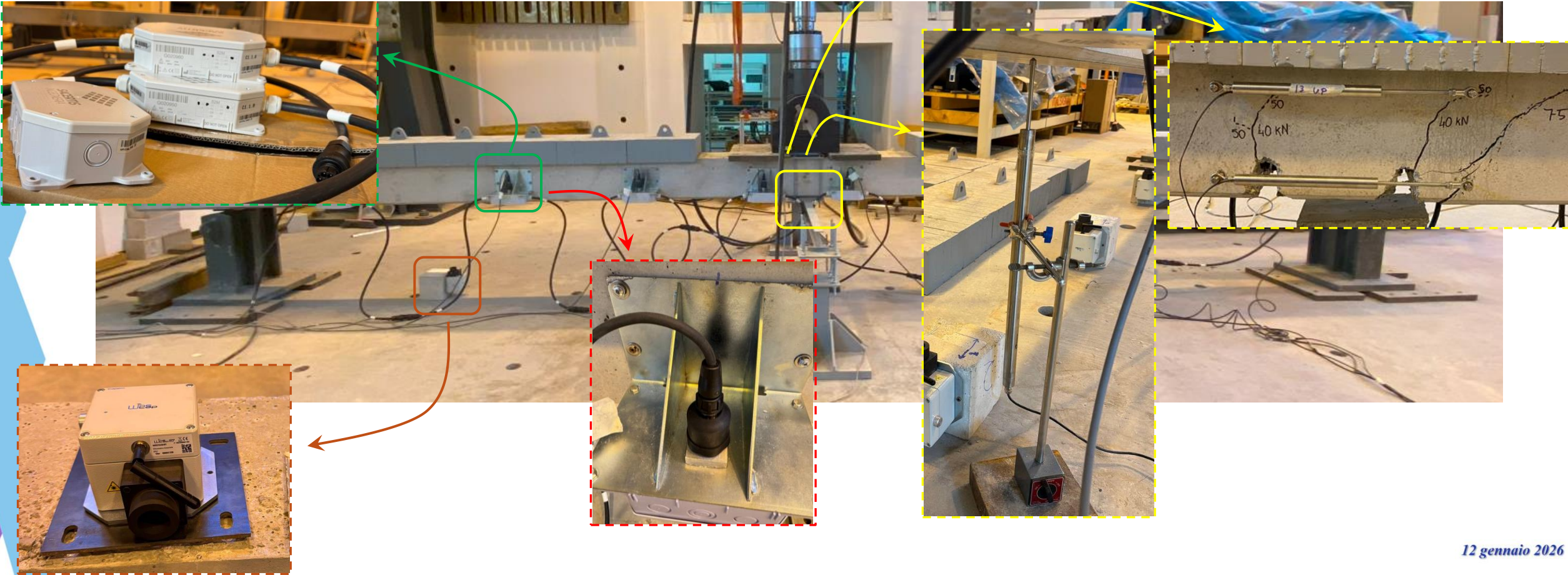
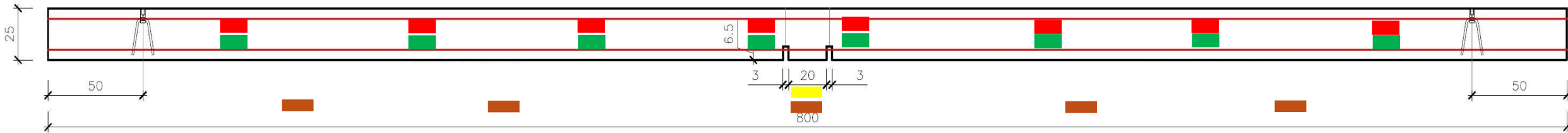
SENSORS' CONFIGURATION

- MEMS (3D Accelerometer + 2D inclinometer)
- Piezoelectric sensor PCB (1D Accelerometer)
- LVDT (for deflection measurements) + crack meters
- LASER (for deflection measurements)

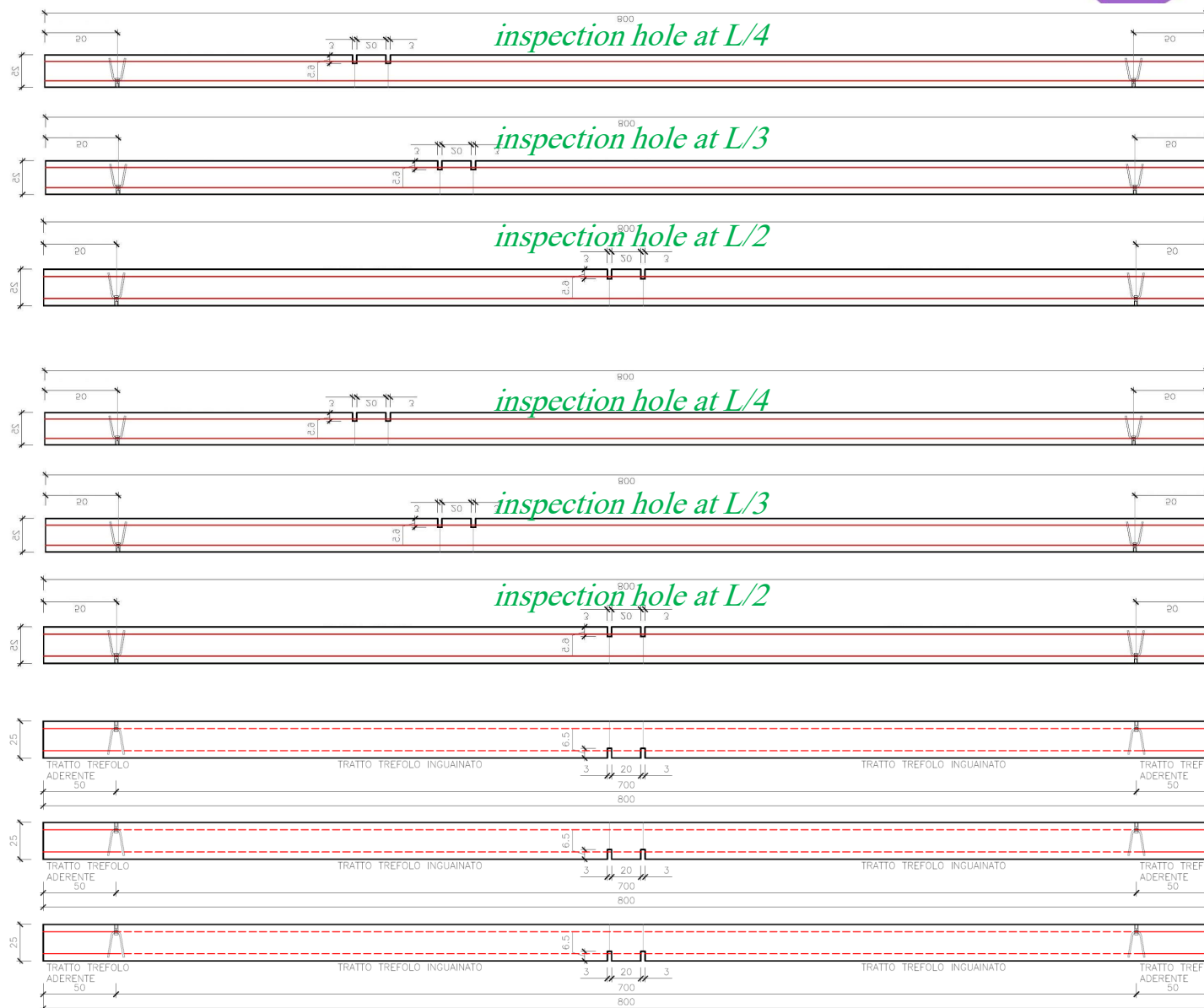


SENSORS' CONFIGURATION

- MEMS (3D Accelerometer + 2D inclinometer)
- Piezoelectric sensor PCB (1D Accelerometer)
- LVDT (for deflection measurements) + crack meters
- LASER (for deflection measurements)



Test Matrix: Bonded & Unbonded Prestressed Beams: Tendon-Cut Damage Scenarios



Bonded Beams

First set: with two-tendon cut damage scenario

D_L_4_2 with 2 cuts

D_L_3_2 with 2 cuts

D_L_2_2 with 2 cuts

Bonded Beams

Second set: with three tendon cut damage scenario

D_L_4_3 with 3 cuts

D_L_3_3 with 3 cuts

D_L_2_3 with 3 cuts

Unbonded Beams

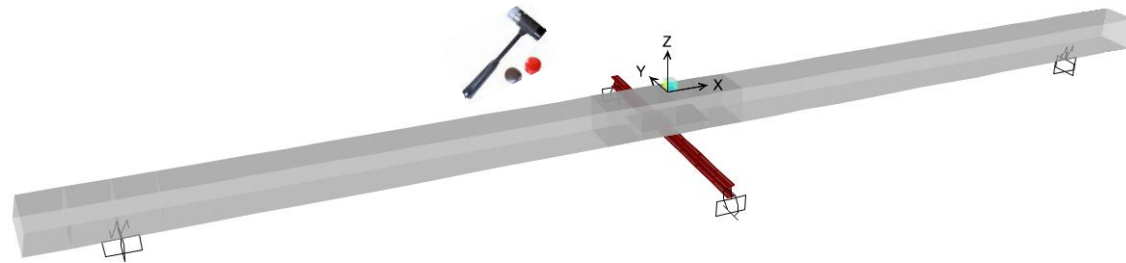
Third set: damage scenario

UB_UD without damage

UB_1 with one strand cut

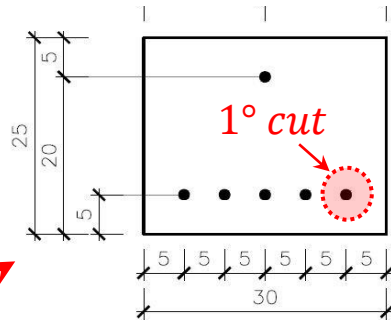
UB_2 with two strand cuts

LOADING CONFIGURATION FOR SLS

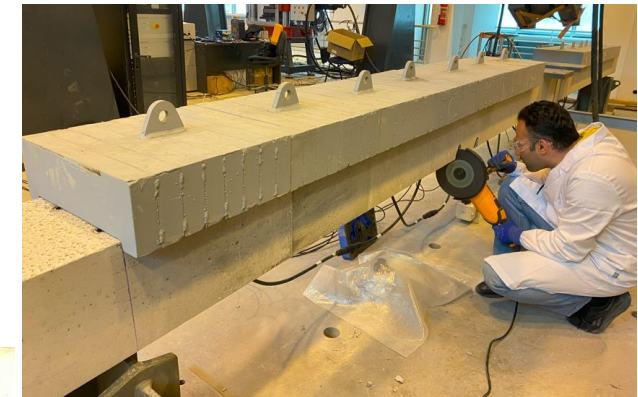
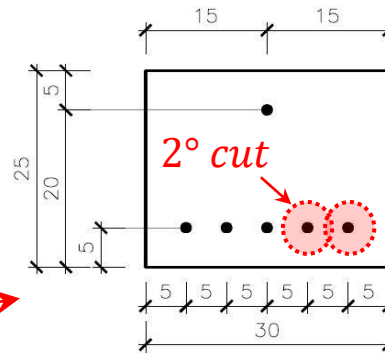


Damage simulation at serviceability conditions
with transverse beam

dynamic test



15kN loading &
unloading, dynamic test

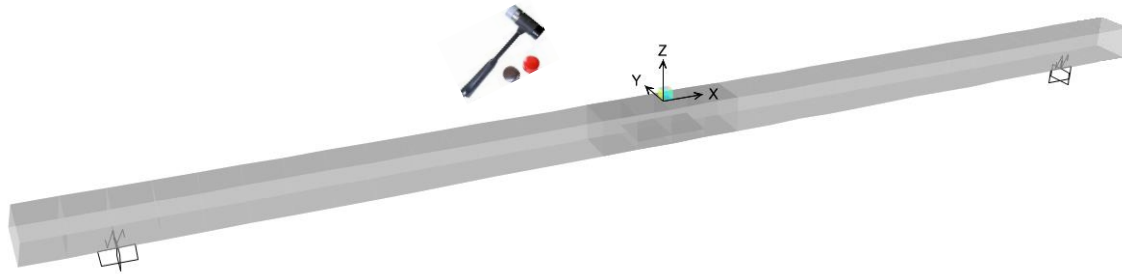


Repeat for the second
inspection hole (2+2 cuts)

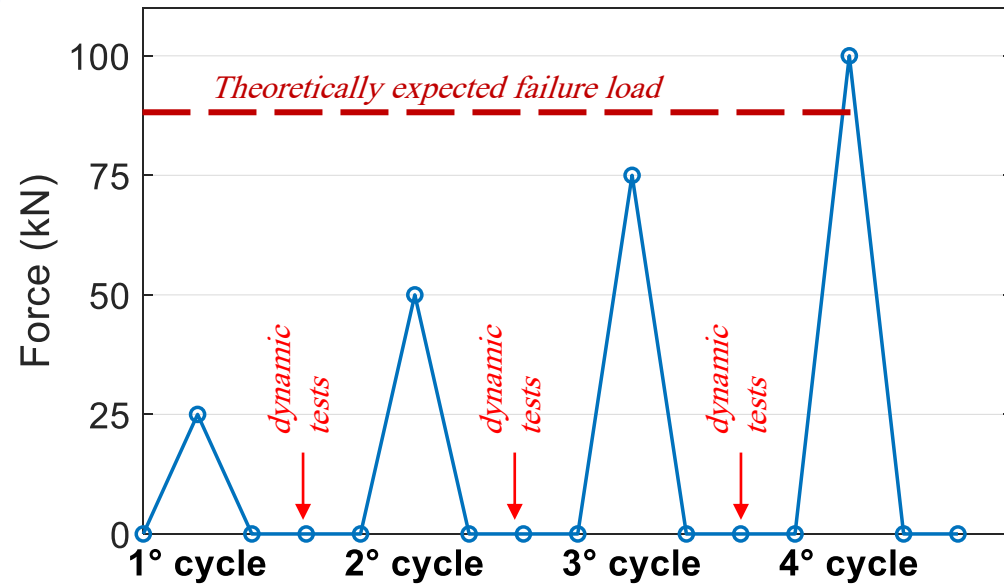


LOADING CONFIGURATION FOR ULS

Damage simulation at ultimate limit states
w/o transverse beam

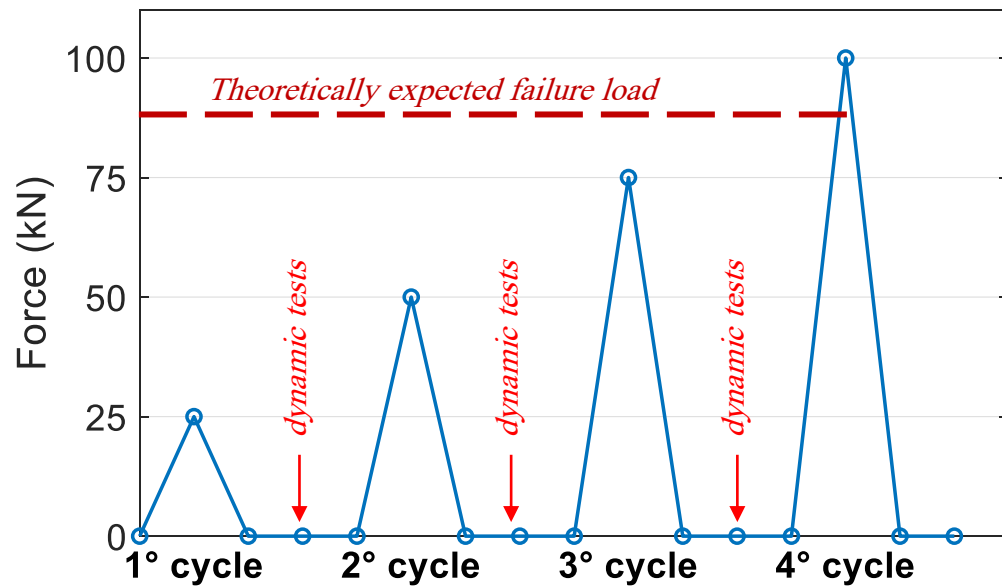
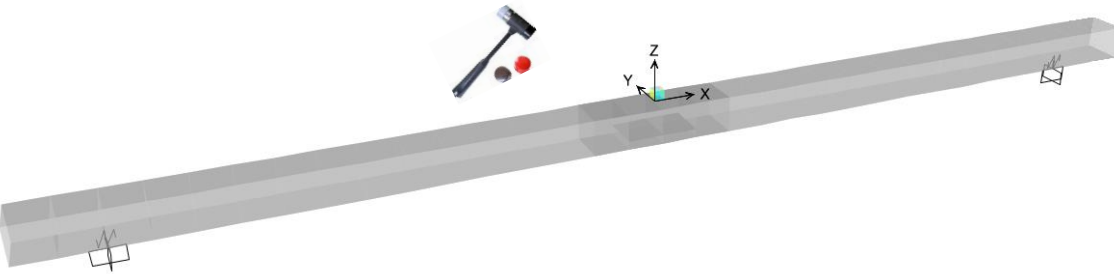


D_L_2_2



LOADING CONFIGURATION FOR ULS

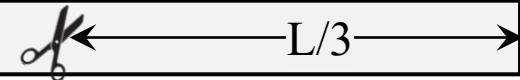
Damage simulation at ultimate limit states
w/o transverse beam



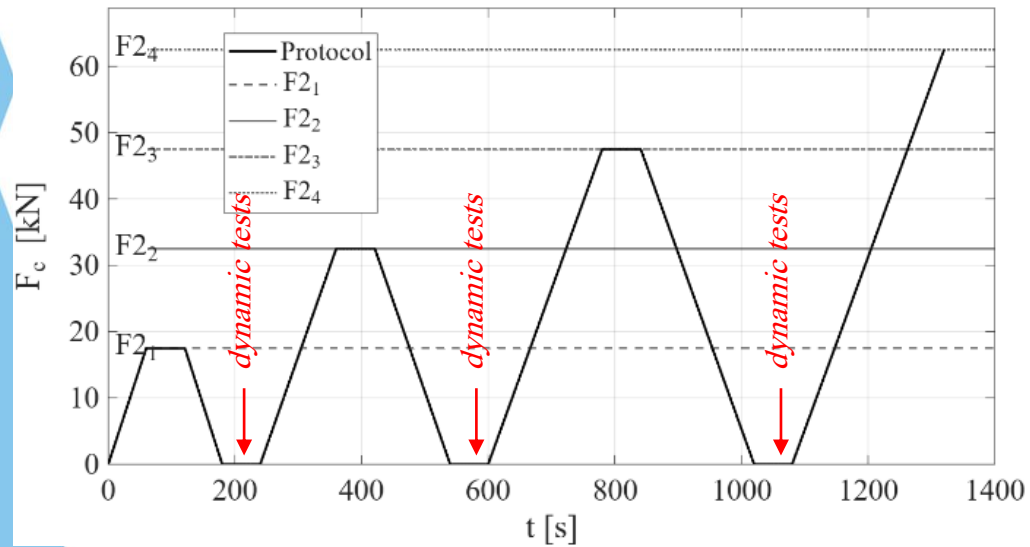
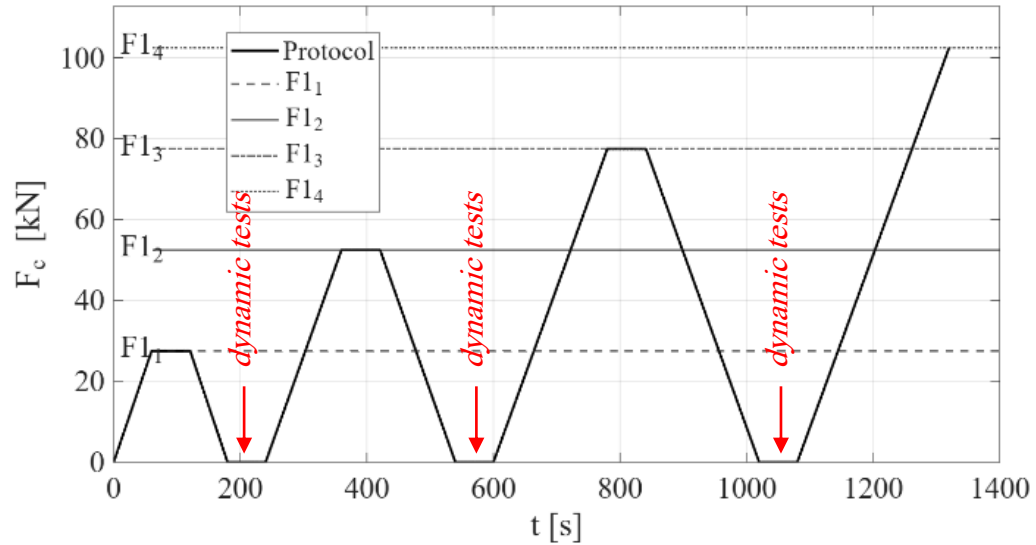
D_L_2_2



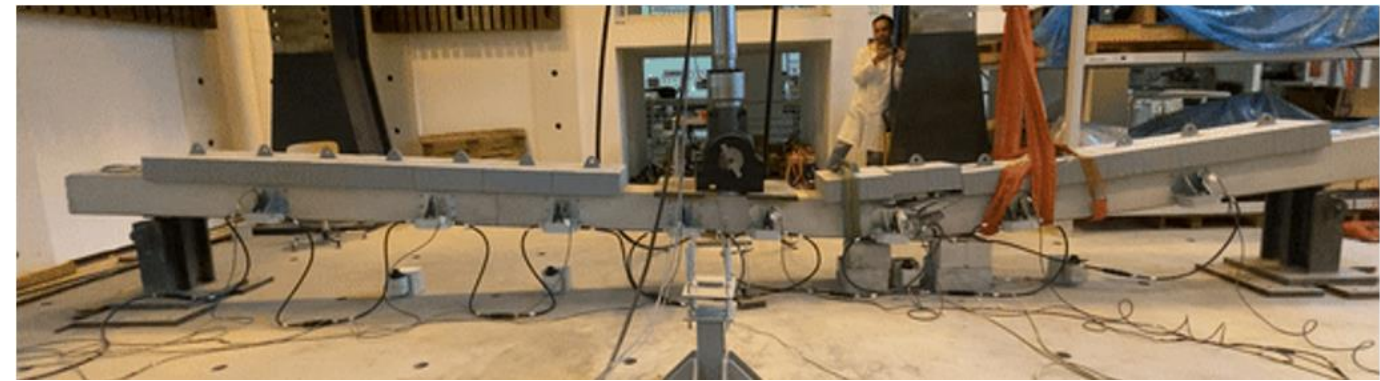
D_L_3_2



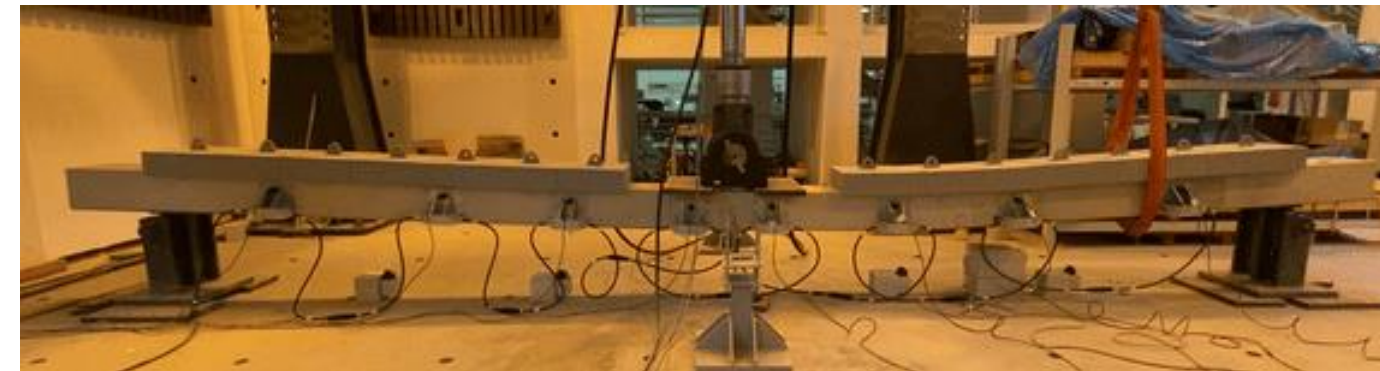
LOADING CONFIGURATION FOR ULS



D_L_2_2 $\leftarrow L/2 \rightarrow$



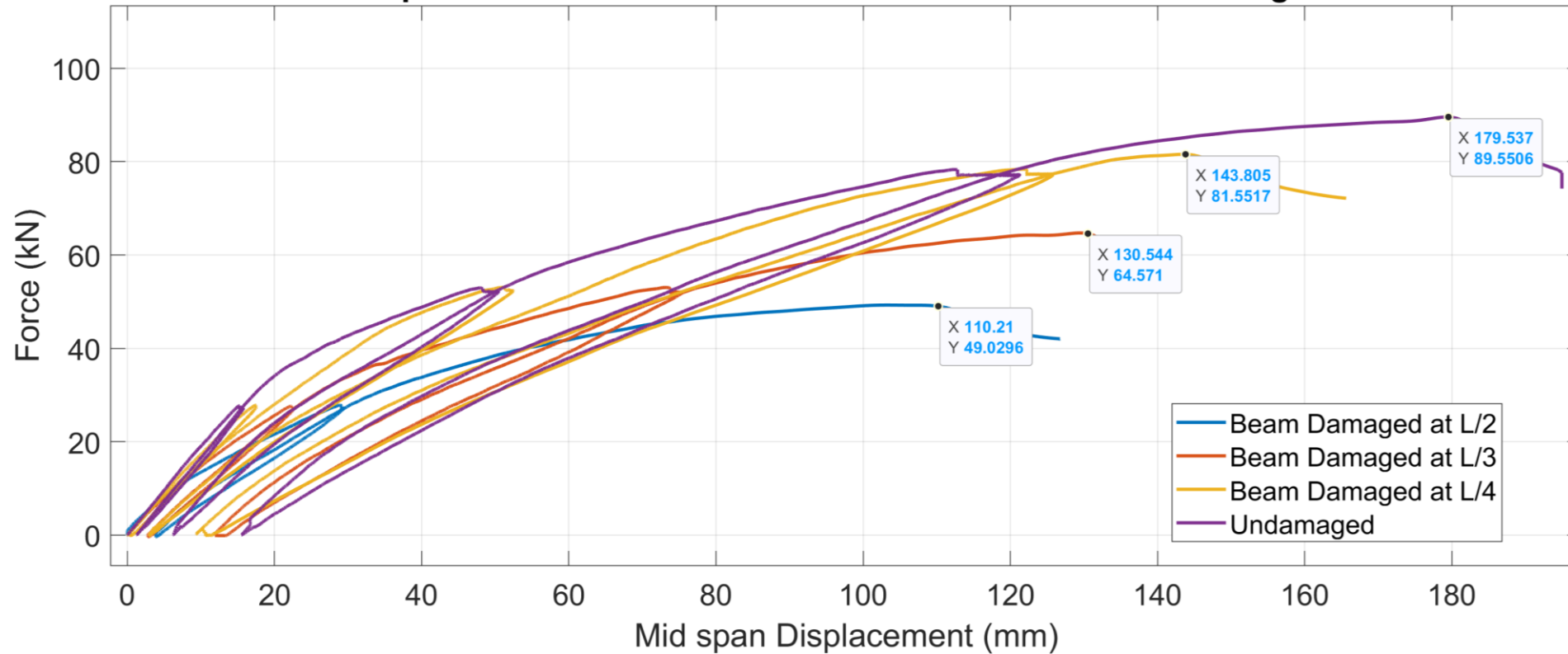
D_L_3_2 $\leftarrow L/3 \rightarrow$



D_L_4_2 $\leftarrow L/4 \rightarrow$

Frist set

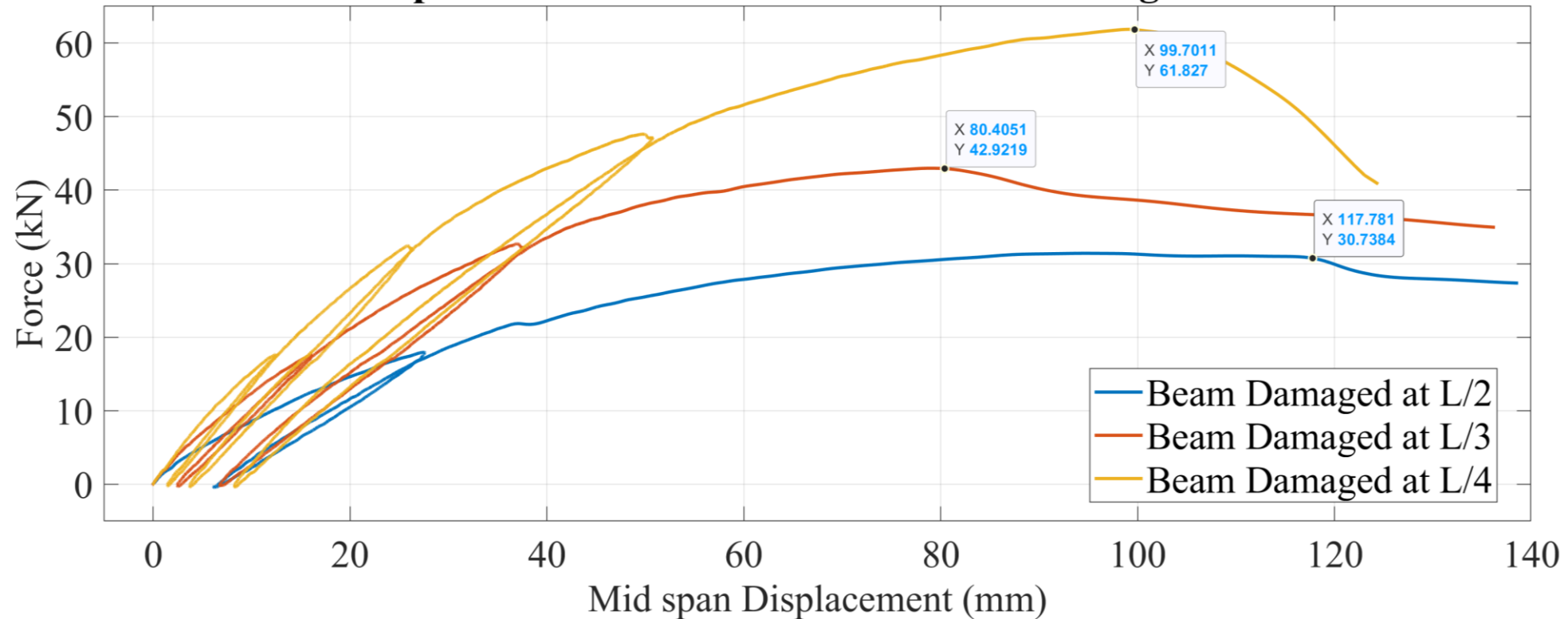
Force-Displacement Curves for Beams with two strand cuts damage scenario



Beam ID	P_{MAX} (kN)	Disp @ P_{MAX} (mm)	Δp (%)	$\Delta disp$ (%)
Undamaged (UD)	89.55	179.12	-	-
D_L_4_2	81.56	143.55	-8.9	-19.9
D_L_3_2	64.71	129.39	-27.7	-27.8
D_L_2_2	49.27	103.13	-45.0	-42.4

Second set

Force-Displacement Curves for Beams with cutting three strands

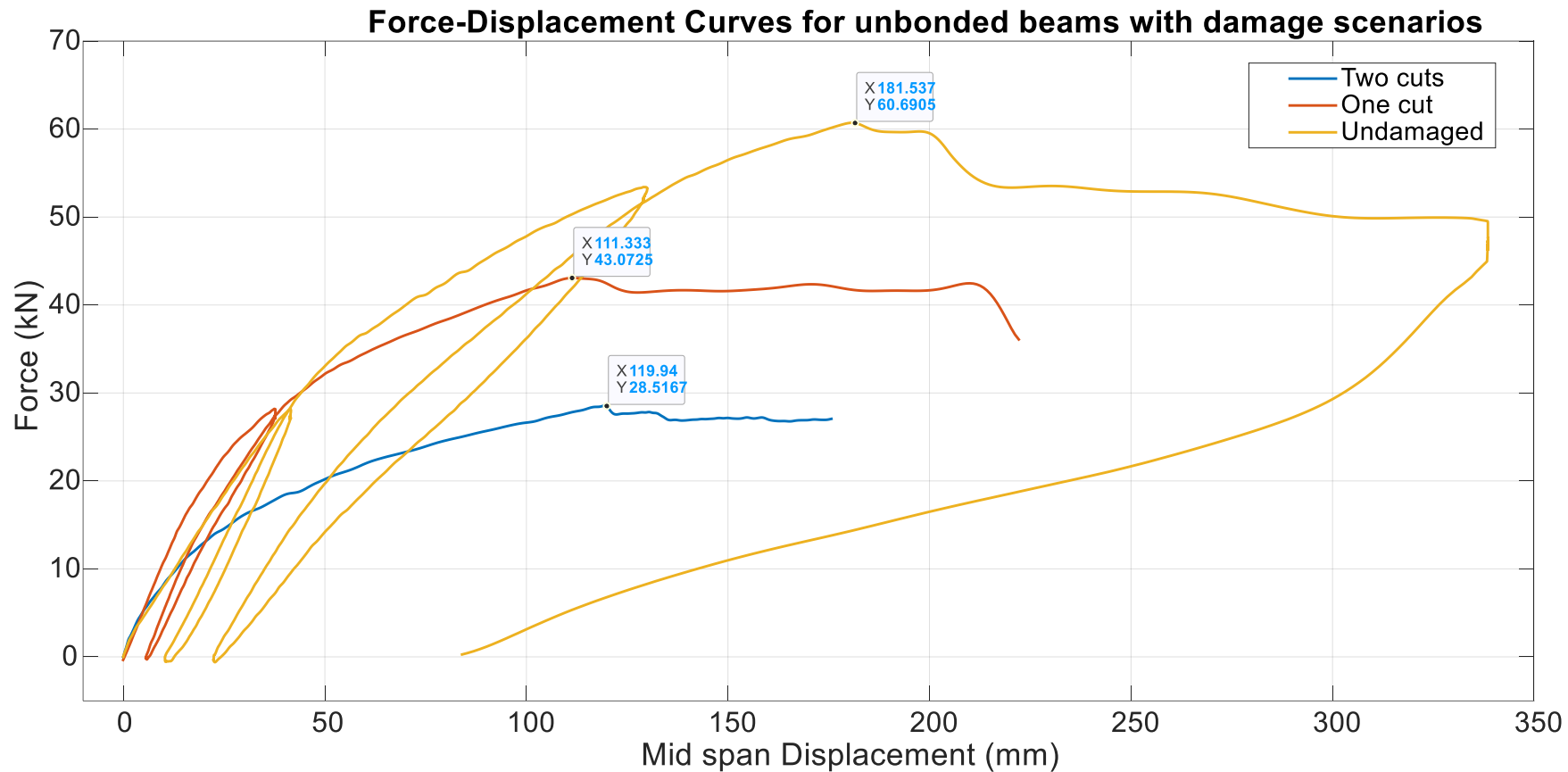


Beam ID	P _{MAX} (kN)	Disp @ P _{MAX} (mm)	Δp (%)	Δ disp (%)
Undamaged (UD)	89.55	179.12	-	-
D_L_4_3	61.82	99.70	-30.96	-44.33
D_L_3_3	42.92	80.40	-52.07	-55.11
D_L_2_3	30.73	117.78	-65.68	-34.24

Comparison of the Force–Displacement Response at Mid-Span for Two Different Damage Scenarios : Frist & Second set

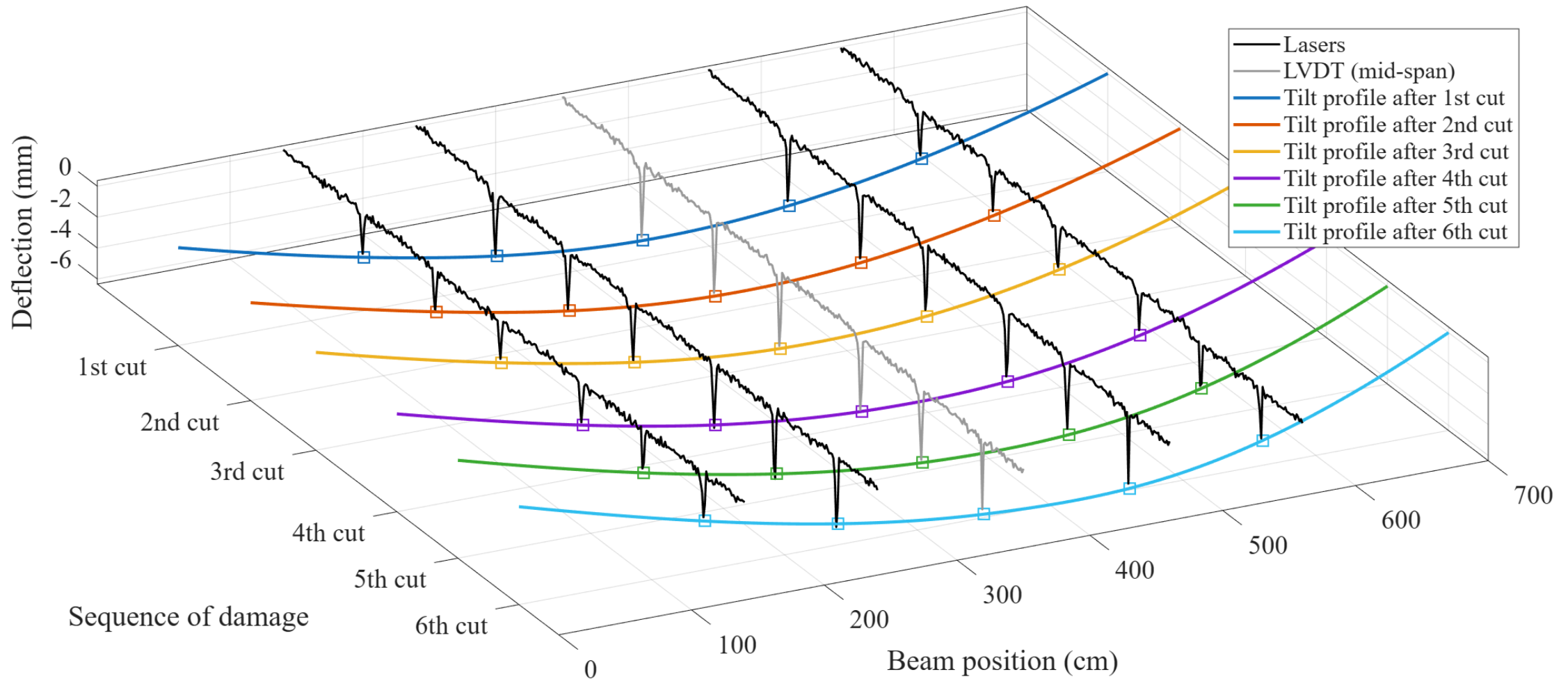
Beam ID	P_{MAX} (kN)	Disp @ P_{MAX} (mm)	Δp (%)	$\Delta disp$ (%)
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D_L_3_2	64.71	129.39	-27.7	-27.8
D_L_3_3	42.92	80.40	-52.07	-55.11
D_L_2_2	49.27	103.13	-45.0	-42.4
D_L_2_2	30.73	117.78	-65.68	-34.24

Third set



Beam ID	P _{MAX} (kN)	Disp @ P _{MAX} (mm)	Δp (%)	Δ disp (%)
Undamaged (UD)	89.55	179.12	-	
UB_UD	60.69	181.53	-32.22	+1.34
UB_1	43.07	111.33	-29.03	-38.67
UB_2	28.51	119.94	-53.02	-33.92

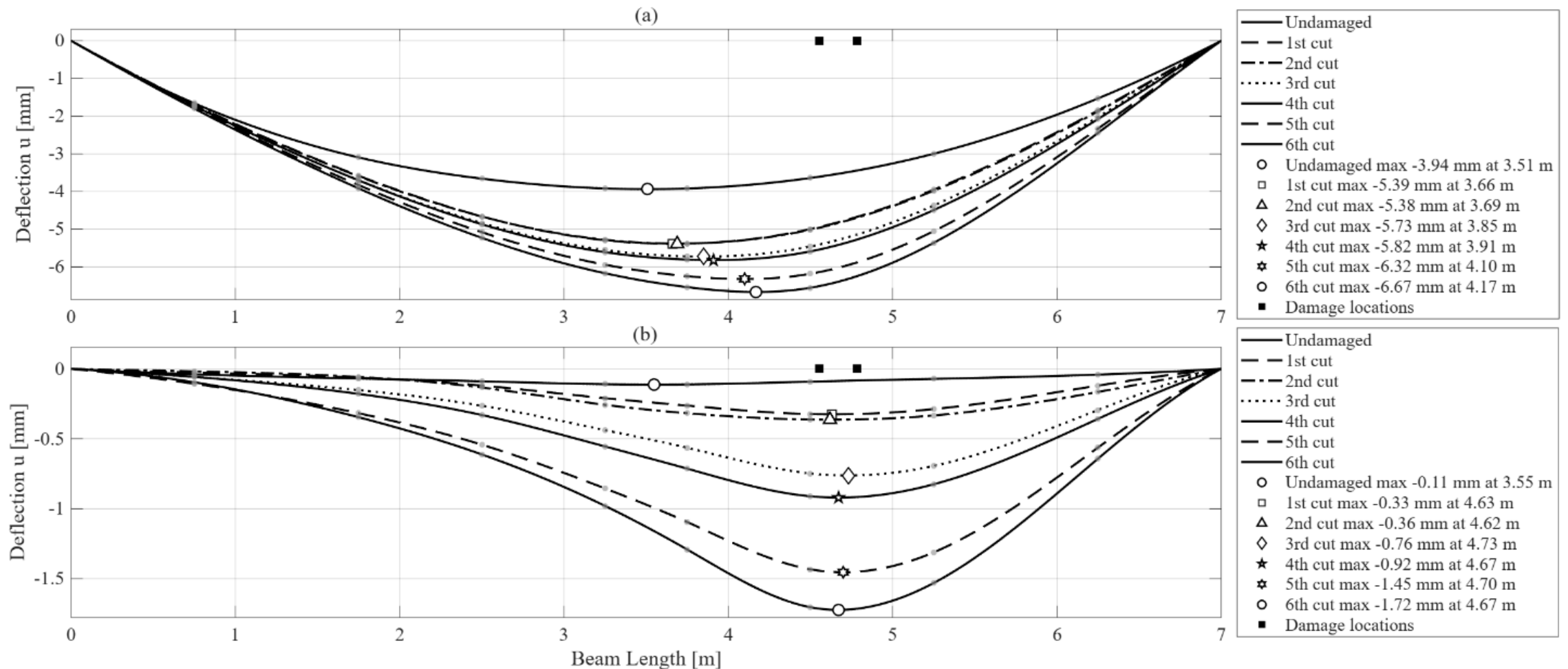
Tilt derived deflection profile validation with Lasers and LVDT



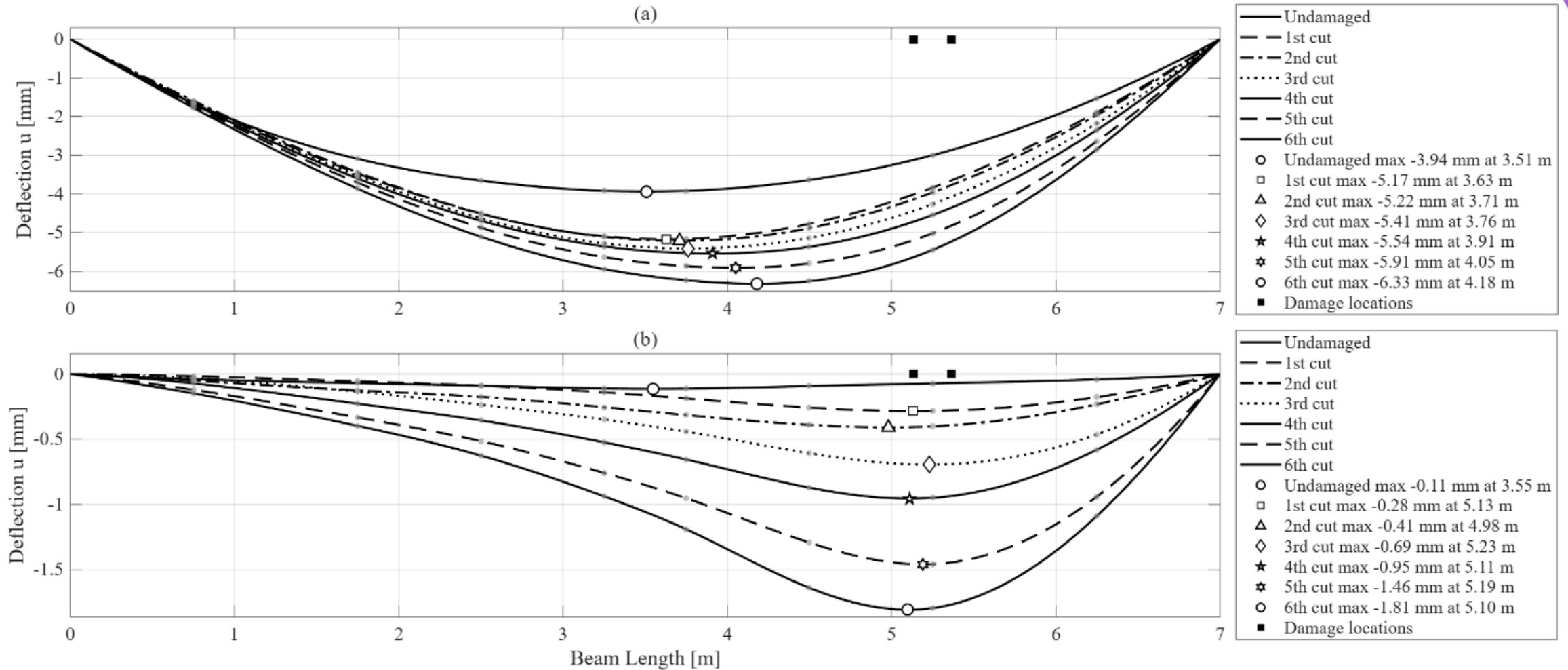
Tilt derived deflection profile validation with Lasers and LVDT

Damage\position	Laser A (1.4m)	Laser B (2.4m)	LVDT (3.5m)	Laser D (4.6m)	Laser E (5.6m)
1-Cut laser-LVDT	-2.71 mm	-4.53 mm	-5.08 mm	-4.45 mm	-3.11 mm
1-Cut Tilt	-2.88 mm	-4.39 mm	-5.16 mm	-4.68 mm	-3.24 mm
1-Cut Error (%)	6.3%	3.1%	1.6%	5.2%	4.1%
2-Cuts laser-LVDT	-2.90 mm	-4.30 mm	-5.11 mm	-4.59 mm	-3.16 mm
2-Cuts Tilt	-2.84 mm	-4.38 mm	-5.19 mm	-4.79 mm	-3.35 mm
2-Cuts Error (%)	2.1%	1.9%	1.6%	4.4%	6.0%
3-Cuts laser-LVDT	-2.74 mm	-4.53 mm	-5.29 mm	-4.71 mm	-3.56 mm
3-Cuts Tilt	-2.92 mm	-4.50 mm	-5.37 mm	-5.05 mm	-3.65 mm
3-Cuts Error (%)	6.6%	0.7%	1.5%	7.2%	2.5%
4-Cuts laser-LVDT	-2.86 mm	-4.83 mm	-5.44 mm	-5.04 mm	-3.66 mm
4-Cuts Tilt	-2.98 mm	-4.57 mm	-5.47 mm	-5.29 mm	-3.92 mm
4-Cuts Error (%)	4.2%	5.4%	0.6%	5.0%	7.1%
5-Cuts laser-LVDT	-2.85 mm	-5.13 mm	-5.71 mm	-5.41 mm	-4.26 mm
5-Cuts Tilt	-3.06 mm	-4.73 mm	-5.78 mm	-5.74 mm	-4.36 mm
5-Cuts Error (%)	7.4%	7.8%	1.2%	6.1%	2.4%
6-Cuts laser-LVDT	-3.00 mm	-5.23 mm	-5.98 mm	-5.97 mm	-4.66 mm
6-Cuts Tilt	-3.18 mm	-4.96 mm	-6.11 mm	-6.20 mm	-4.72 mm
6-Cuts Error (%)	6.0%	5.2%	2.2%	3.9%	1.3%
MAPE (%)	5.4%	4.0%	1.5%	5.3%	3.9%

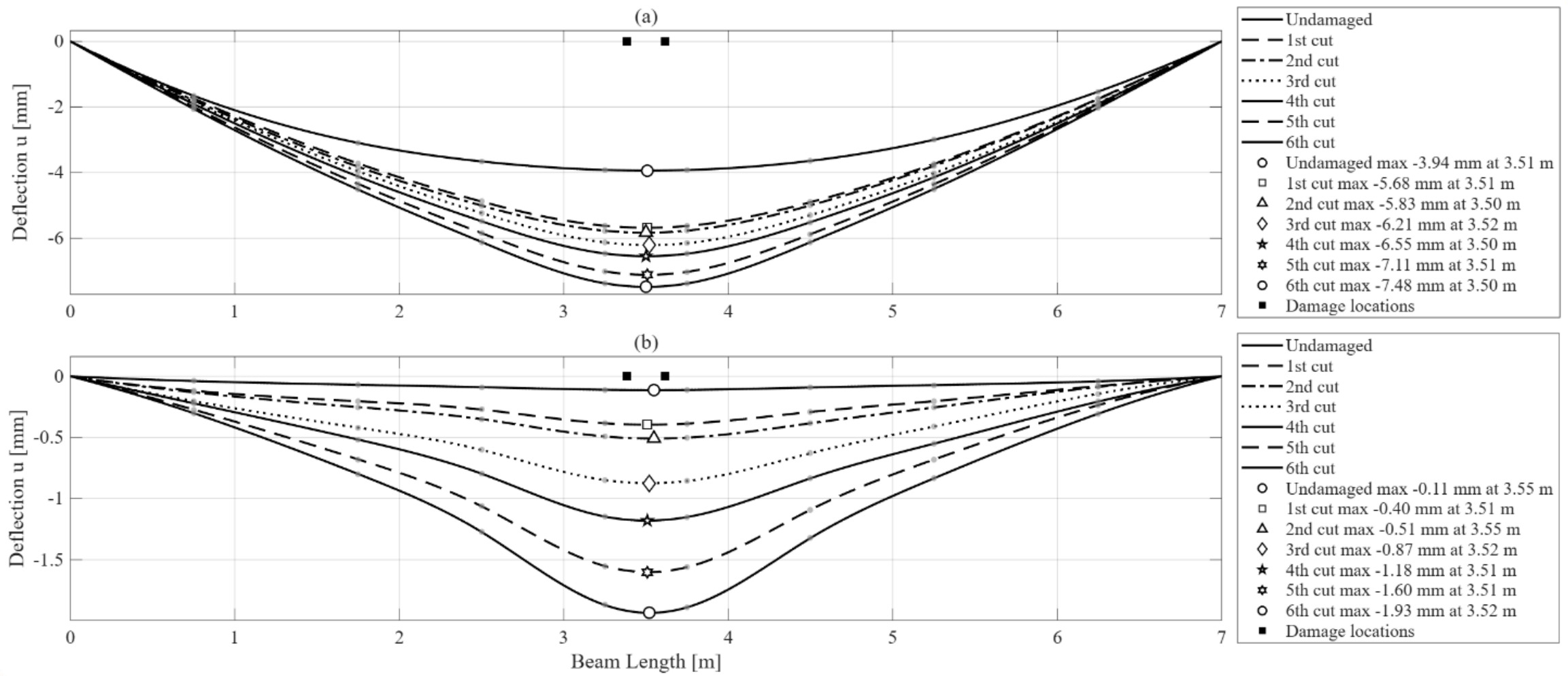
D_L_3_3 deflection profile from tilt during loading of 15 kN
at mid-span (a) and unloading (b)



D_L_4_3 deflection profile from tilt during loading of 15 kN at mid-span (a) and unloading (b)



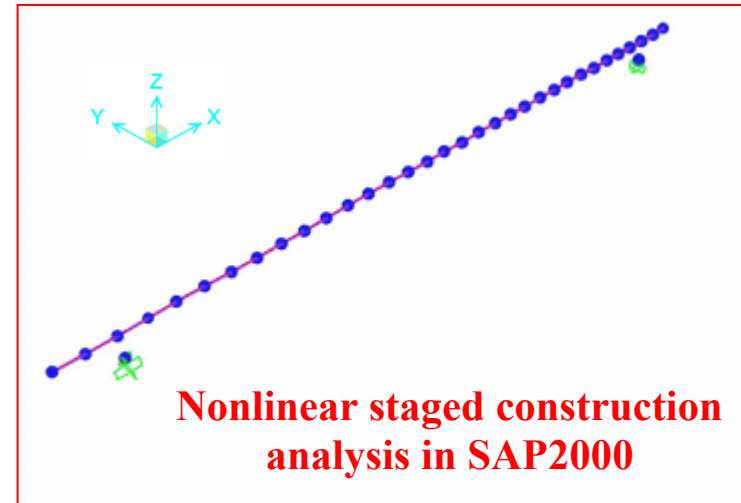
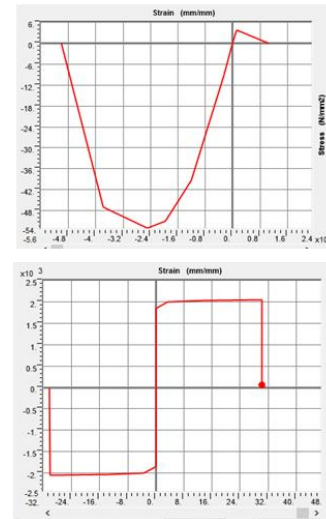
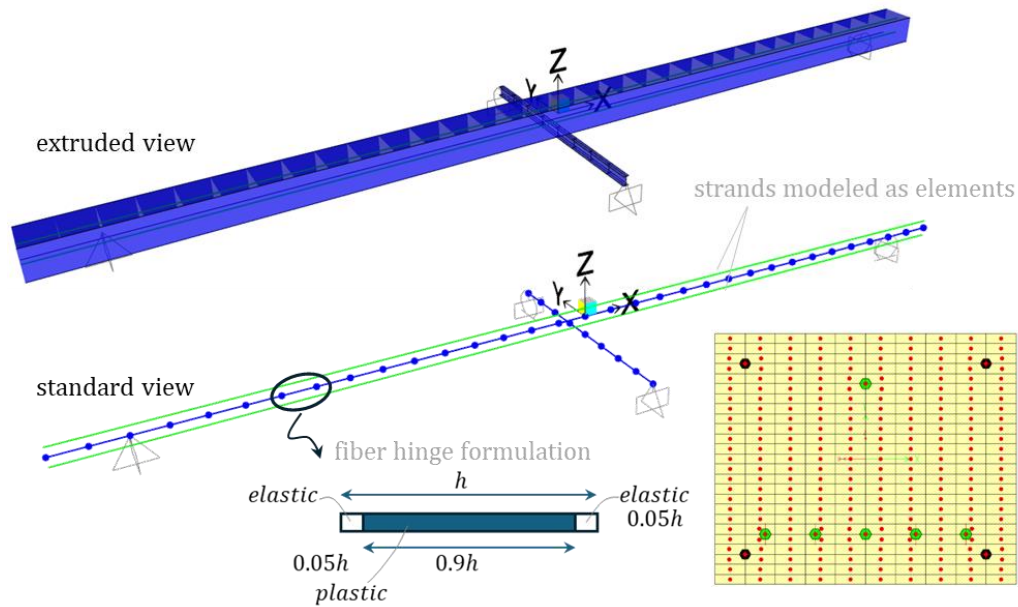
D_L_2_3 deflection profile from tilt during loading of 15 kN at mid-span (a) and unloading (b)



Comparison of the residual deflection and related location for the second damage scenario with increasing damage

Damage/Beam type	D_L/2_3 damage at x = 3.5m		D_L/3_3 damage at x = 4.67m		D_L/4_3 damage at x = 5.25m	
	u_{res}^{max} (mm)	x_{max}^{load} (m)	u_{res}^{max} (mm)	x_{max}^{load} (m)	u_{res}^{max} (mm)	x_{max}^{load} (m)
After 1 cut	-0.40	3.51	-0.33	4.63	-0.28	5.13
After 2 cuts	-0.51	3.55	-0.36	4.62	-0.41	4.98
After 3 cuts	-0.87	3.52	-0.76	4.73	-0.66	5.23
After 4 cuts	-1.18	3.51	-0.92	4.67	-0.95	5.11
After 5 cuts	-1.60	3.51	-1.45	4.70	-1.46	5.19
After 6 cuts	-1.93	3.52	-1.72	4.67	-1.81	5.10

NUMERICAL MODELING



Mode shapes of PC beams with steel blocks w/o transverse beam

	Mode-1	Mode-2(L)	Mode-3(L)	Mode-4	Mode-5
Enhanced FEM	7.20	8.84	17.96	20.25	43.19
Undamaged_(MEMS)	7.17	8.43	18.16	19.54	44.25
FBG-undamaged	7.20	8.72	-	19.46	43.63

Curvature Damage Factor (CDF)

$$\text{CDF} = \frac{1}{N} \sum_{i=1}^N |v''_{o,i} - v''_{d,i}|$$

Curvature Damage Factor (CDF)

N is total number of modes

v''_o is the undamaged curvature mode shape

v'_d is the damaged curvature mode shape

DAMAGE DETECTION IN BRIDGES USING MODAL CURVATURES: APPLICATION TO A REAL DAMAGE SCENARIO
by G. DE ROECK, M. M. ABDEL WAHAB, 1999, Journal of Sound and Vibration

$$\text{SDF} = \frac{1}{N} \sum_{i=1}^N |v'_{o,i} - v'_{d,i}|$$

Slope Damage Factor (SDF)

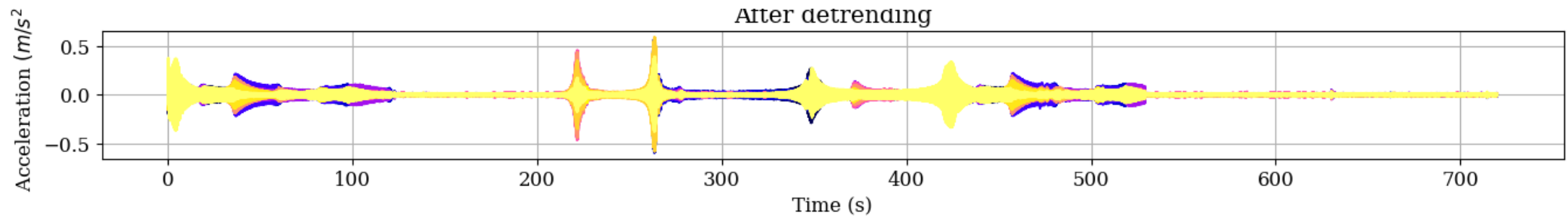
N is total number of modes

v''_o is the undamaged slope mode shape

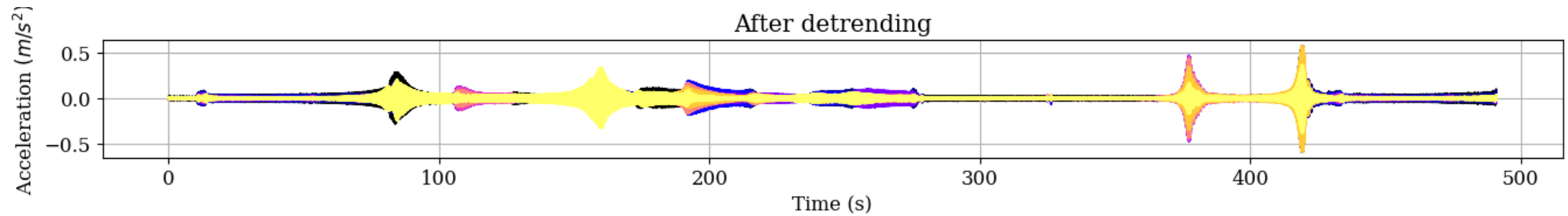
v'_d is the damaged slope mode shape

Time History of accelerations for MEMS & PCB

MEMS

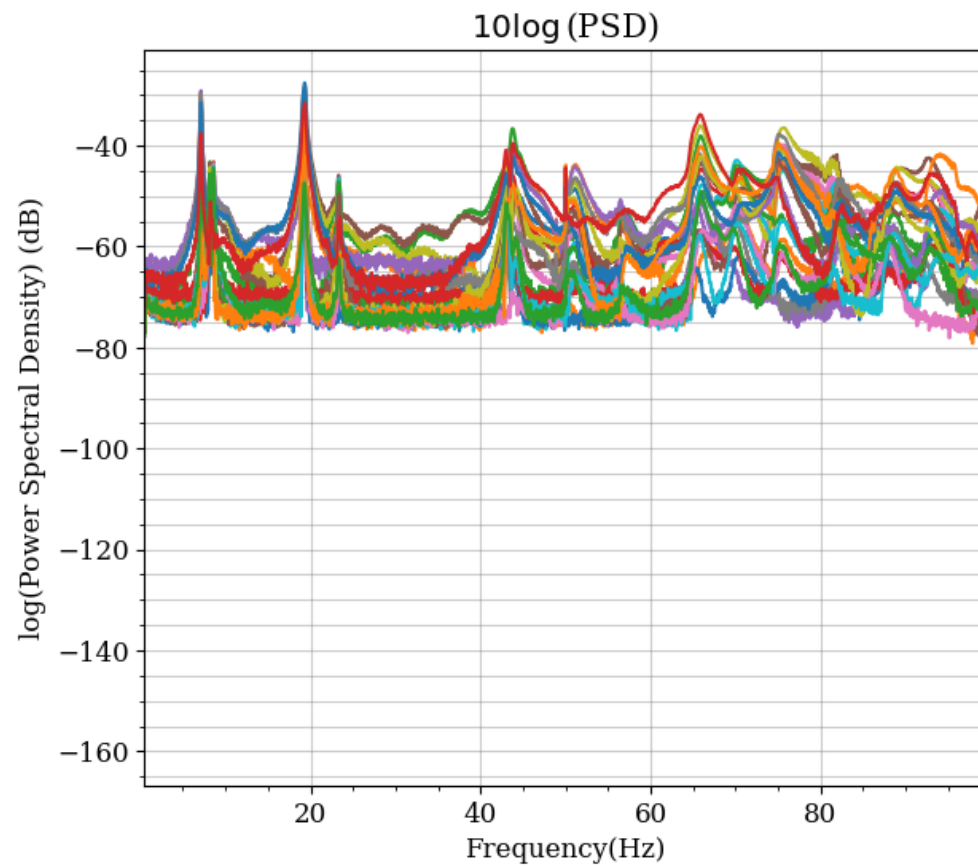


PCB

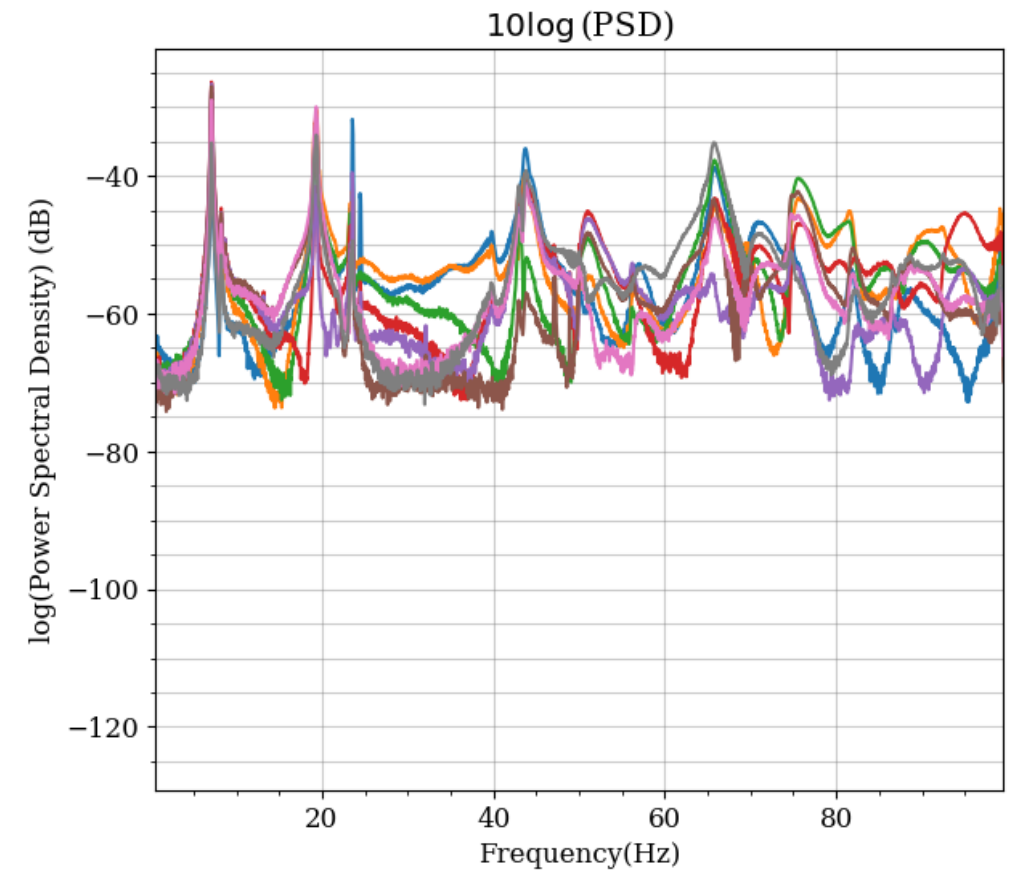


PSD comparison

MEMS

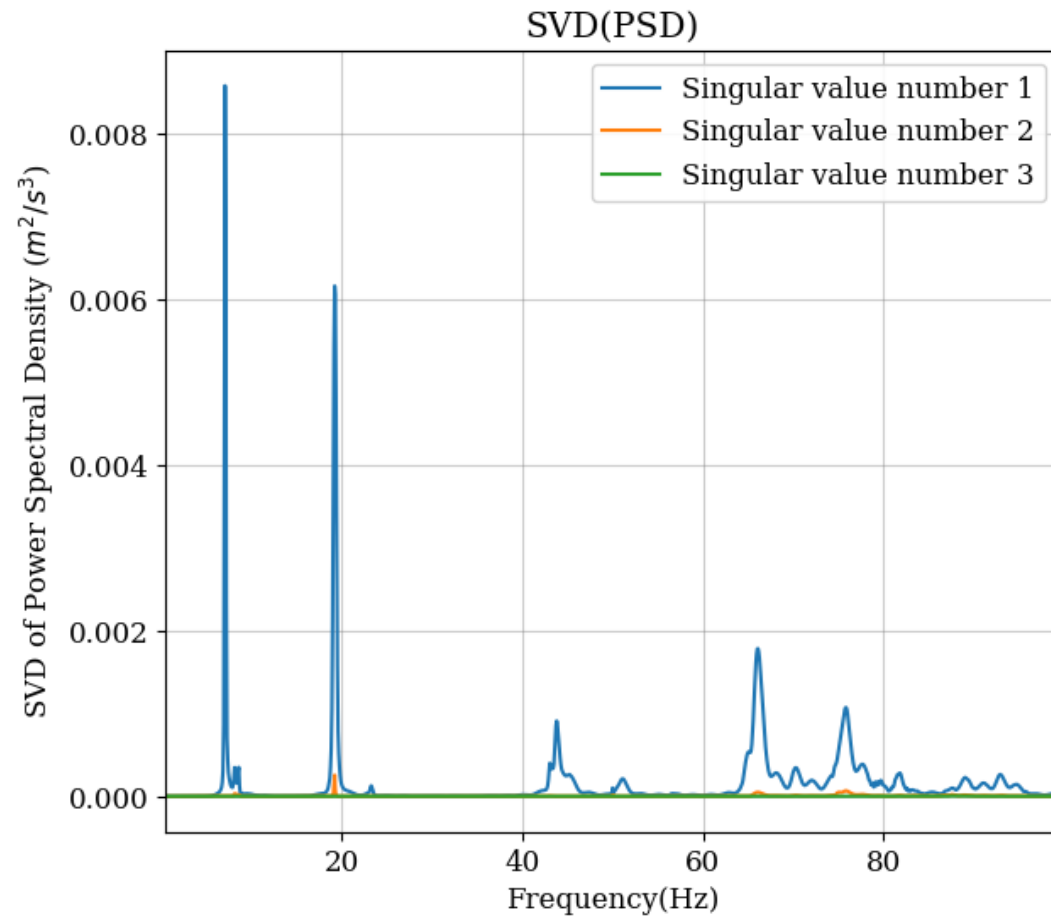


PCB

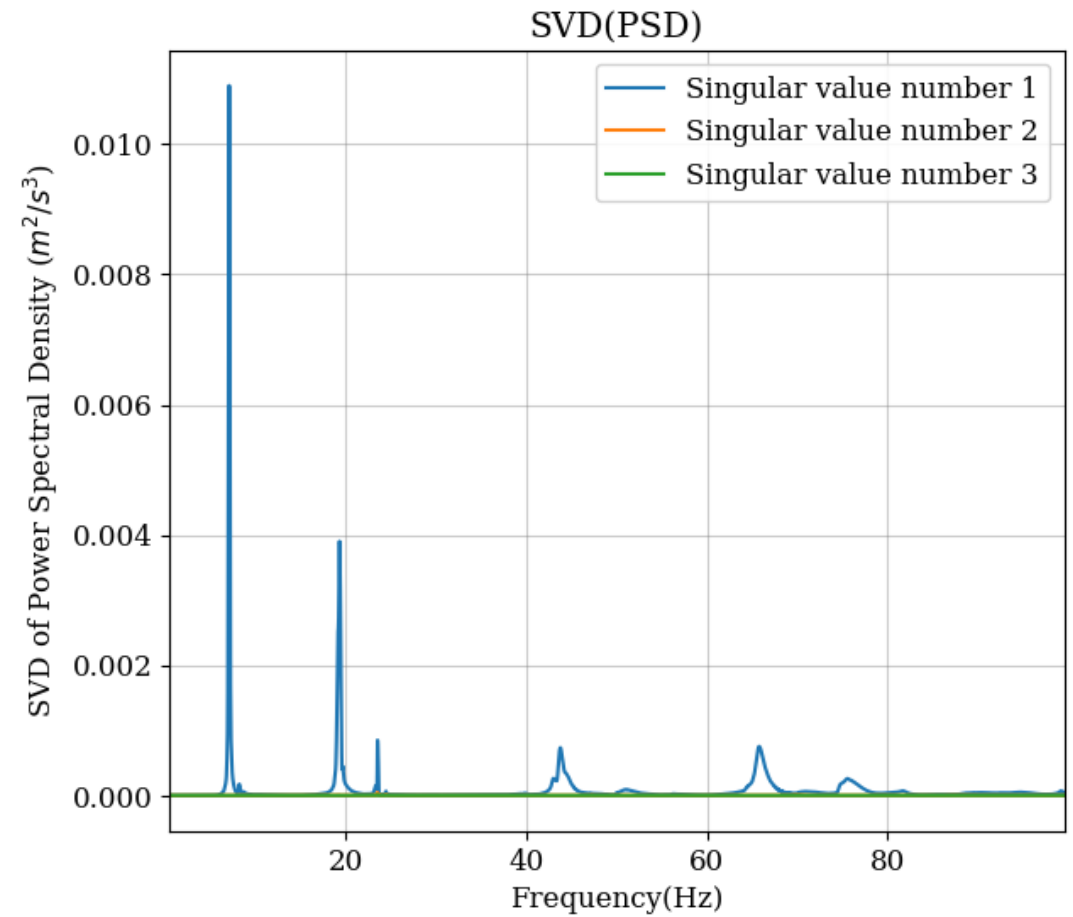


SVD comparison

MEMS

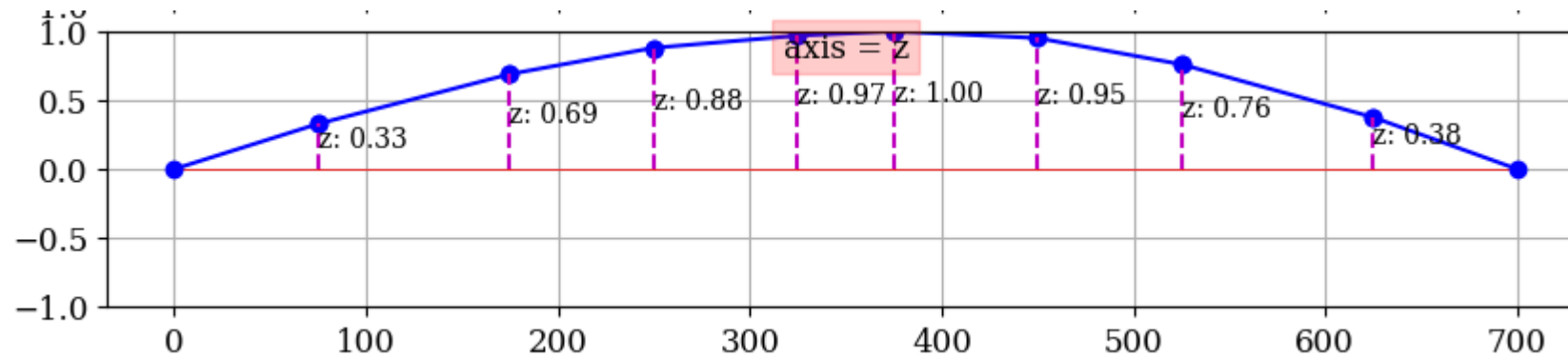


PCB

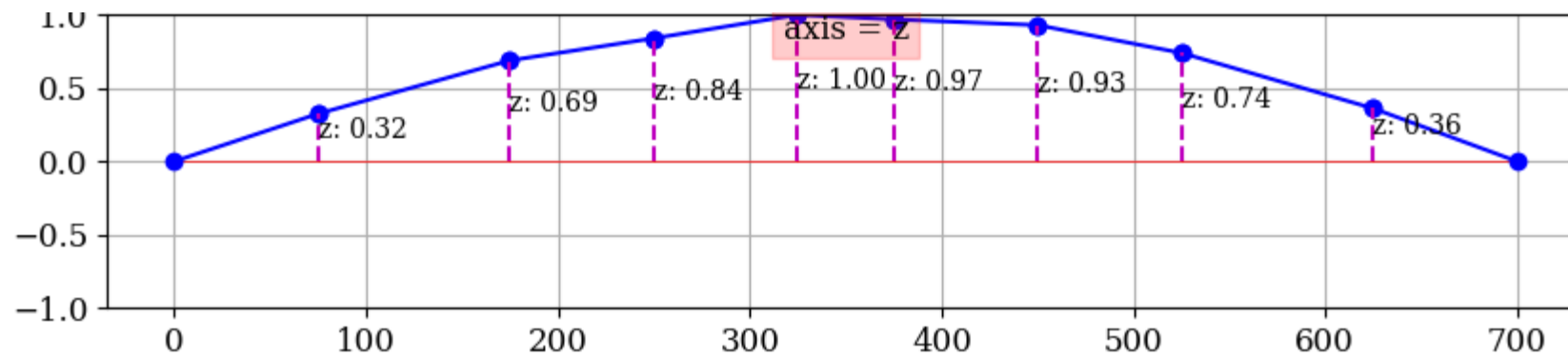


1st Bending mode (7.11 Hz)

MEMS

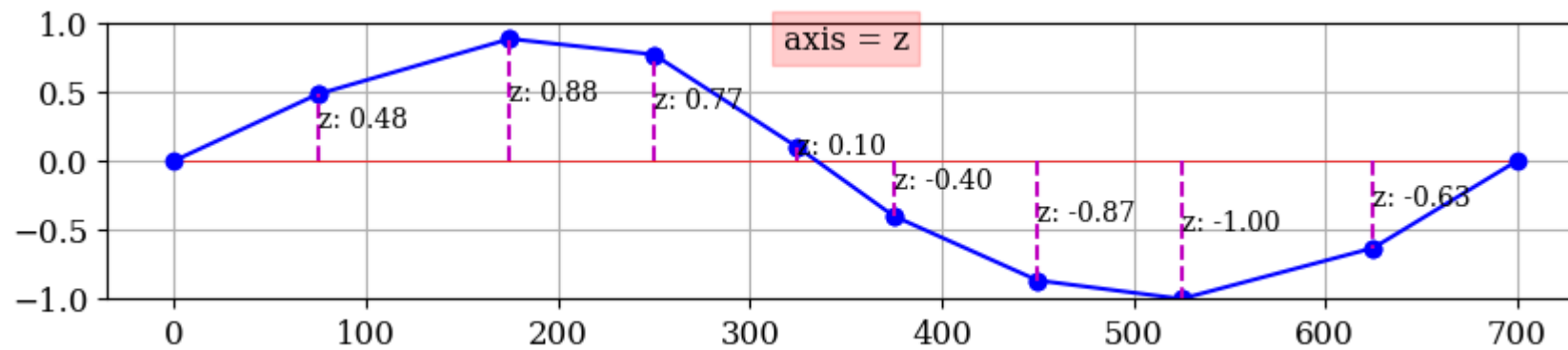


PCB

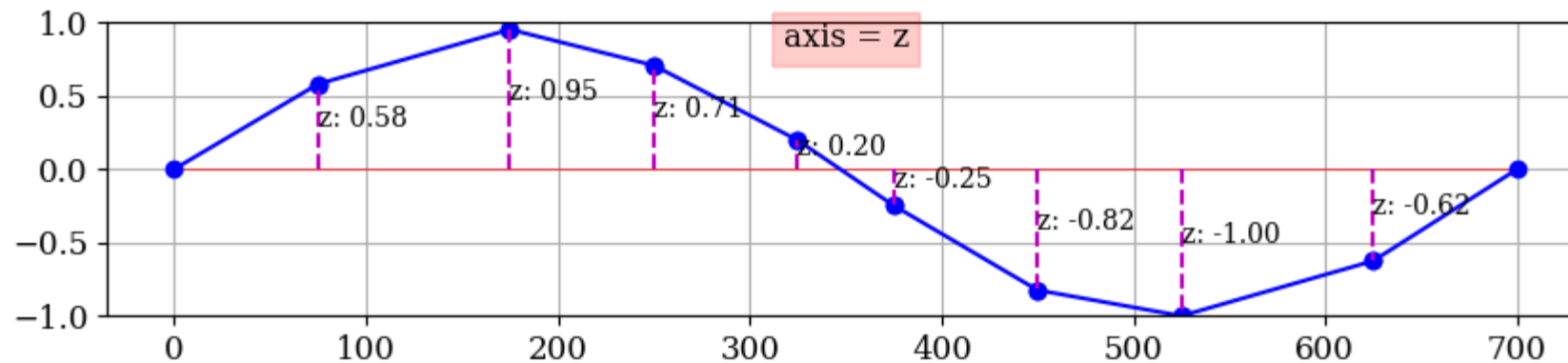


2nd Bending mode (19.31 Hz)

MEMS

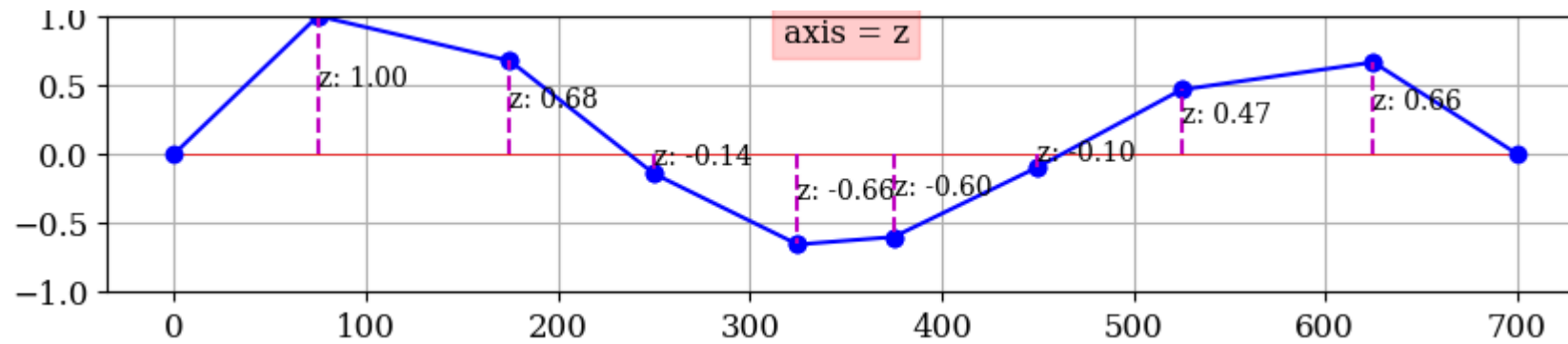


PCB

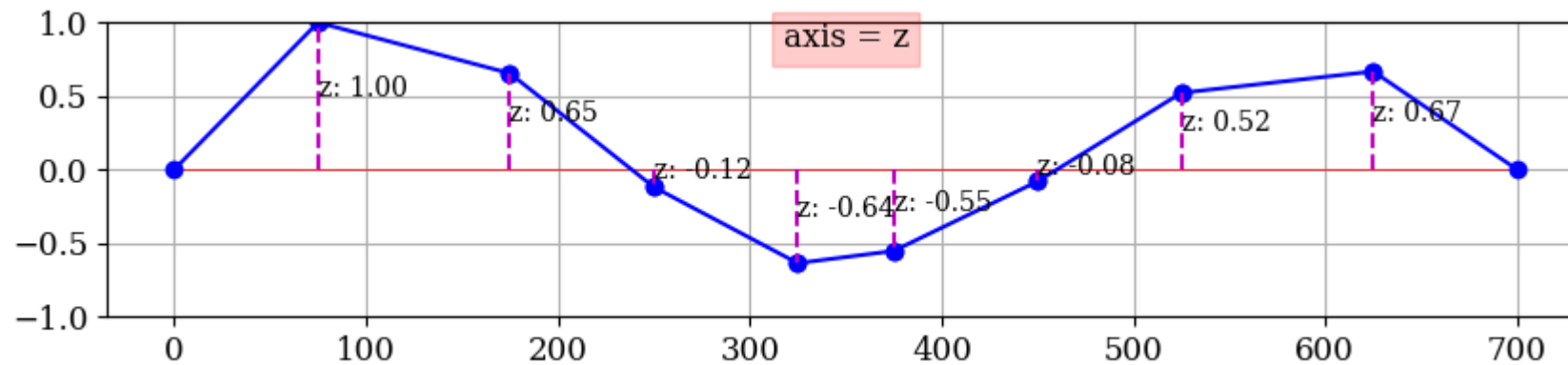


3rd Bending mode (43.76 Hz)

MEMS

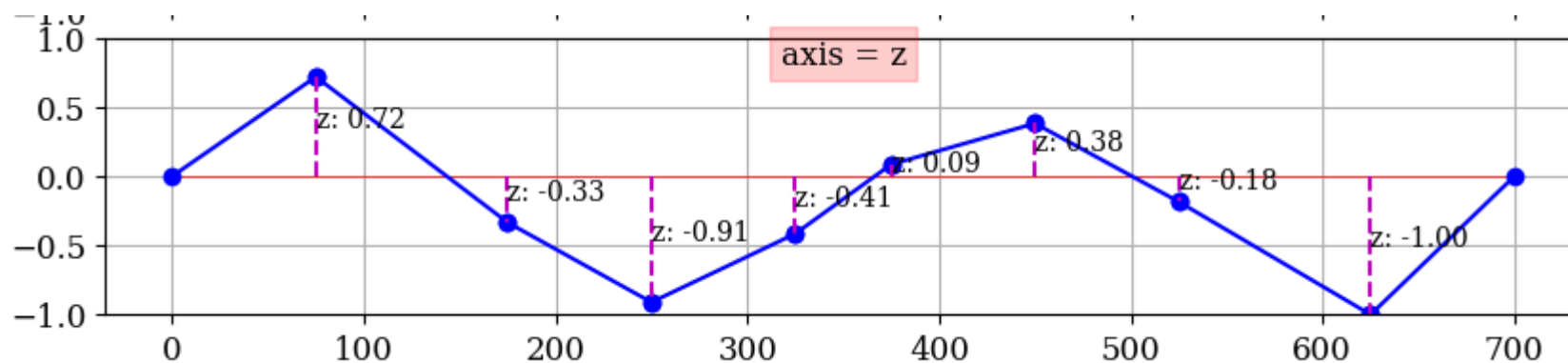


PCB

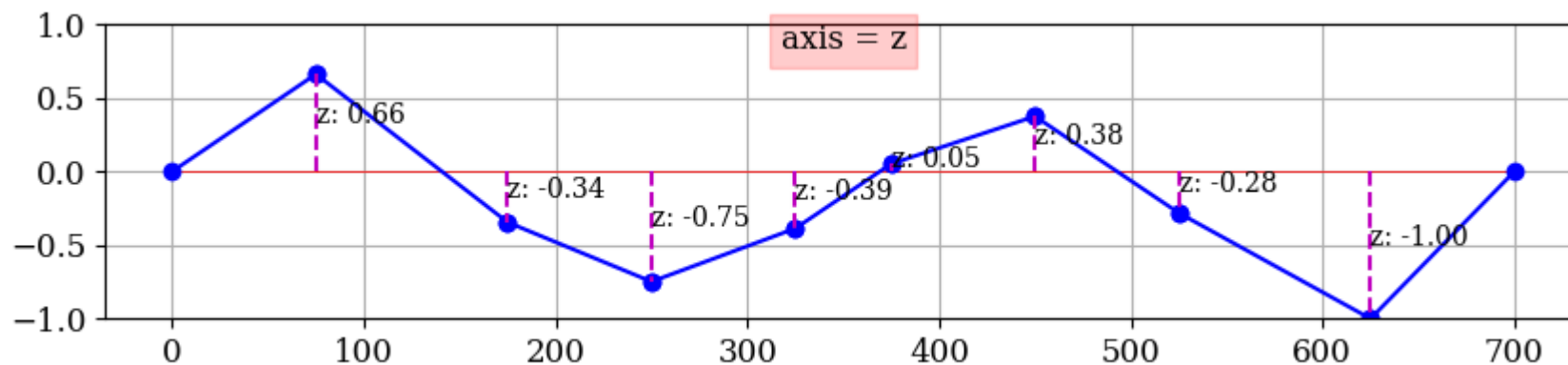


4th Bending mode (69.00 Hz)

MEMS



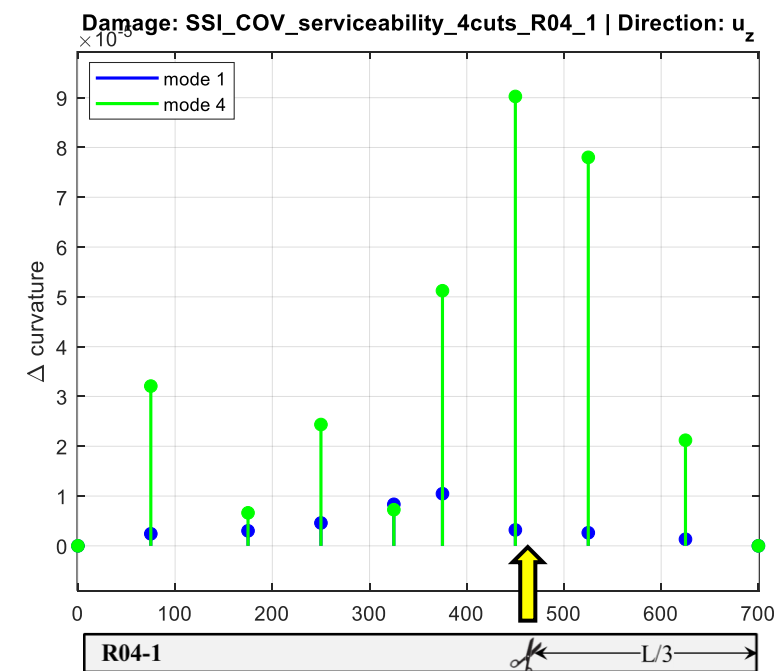
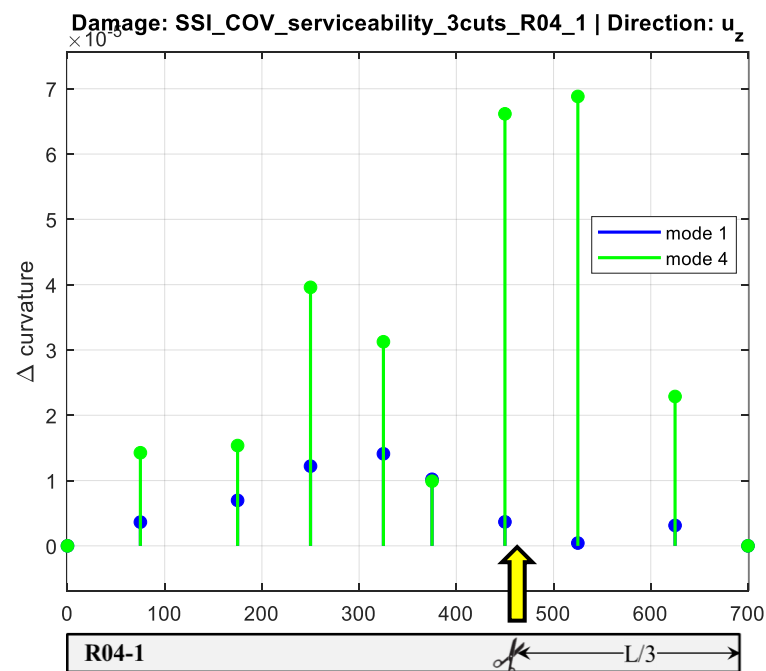
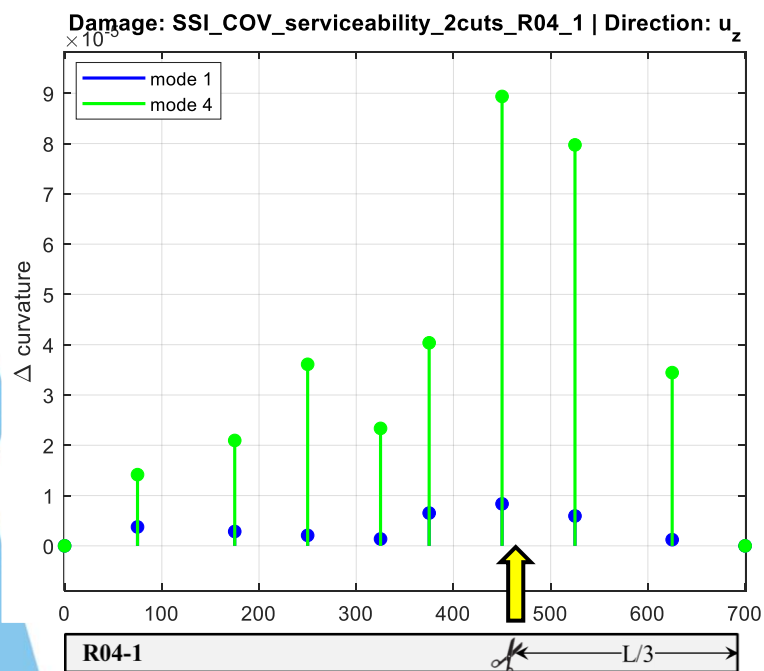
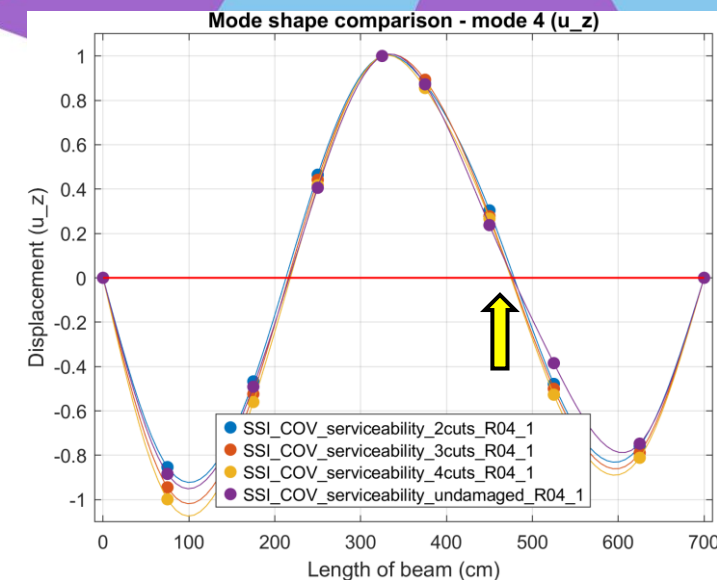
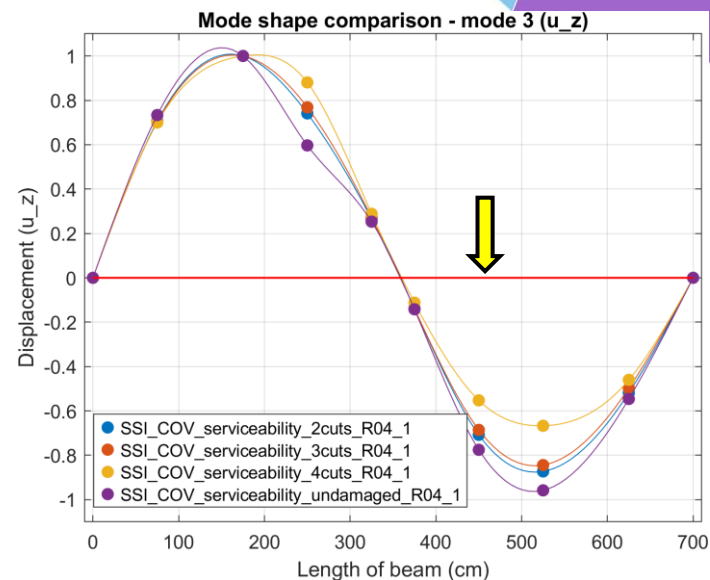
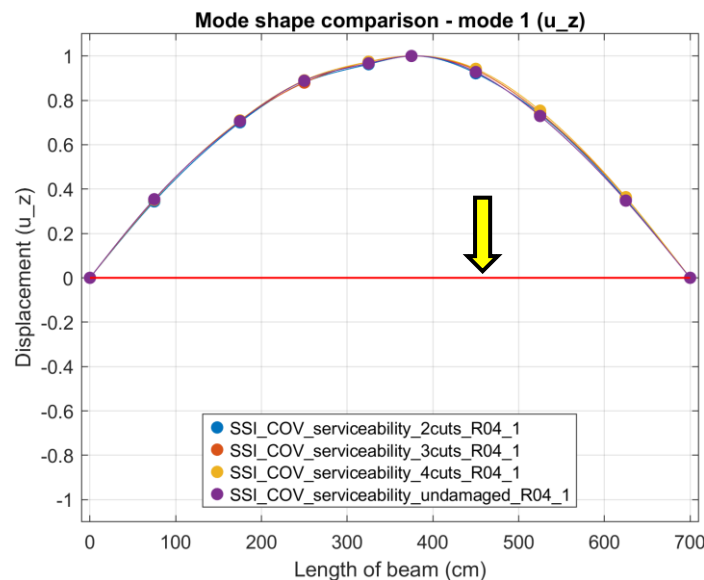
PCB



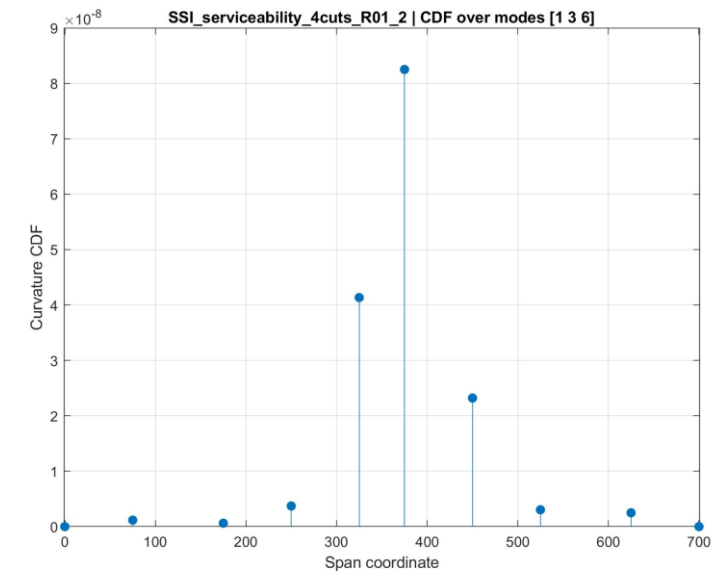
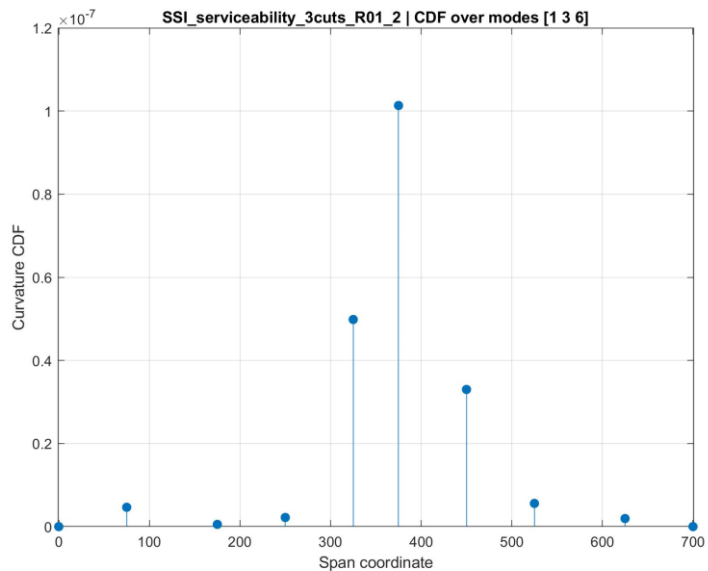
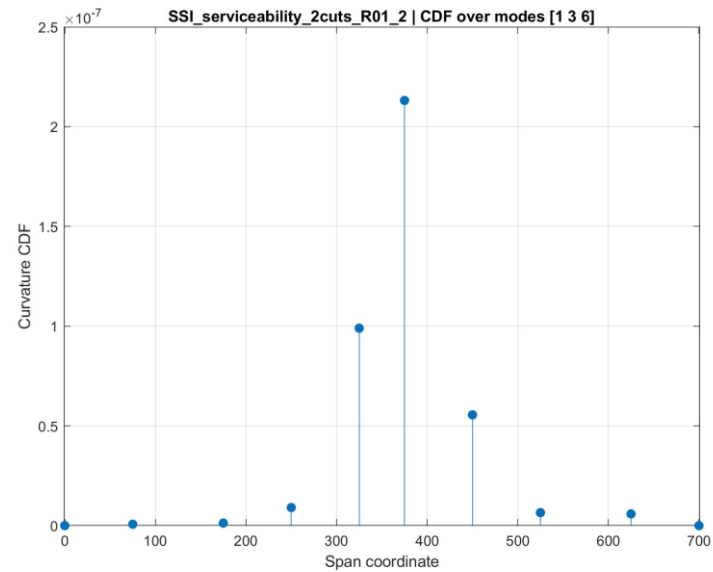
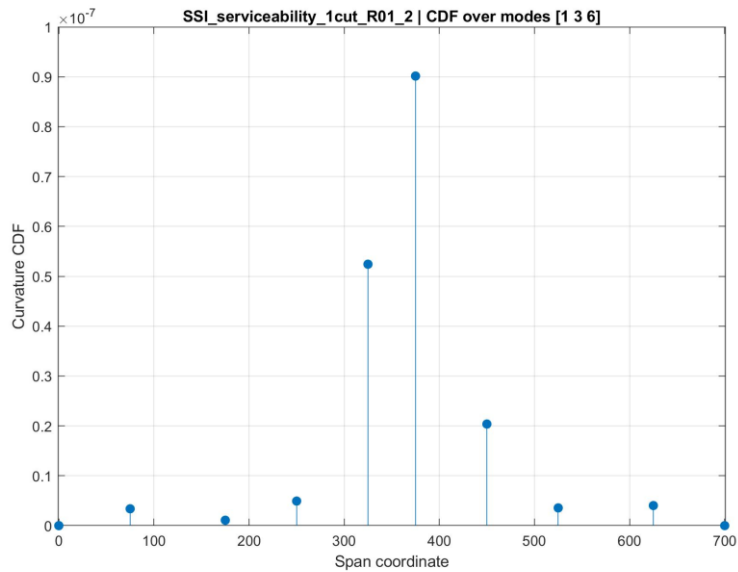
RESULTS AT SLS – MODAL CURVATURE COMPARISON

R04-1

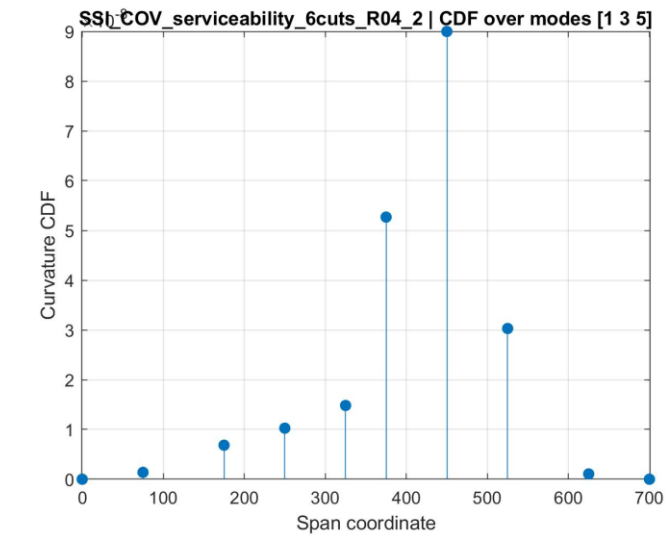
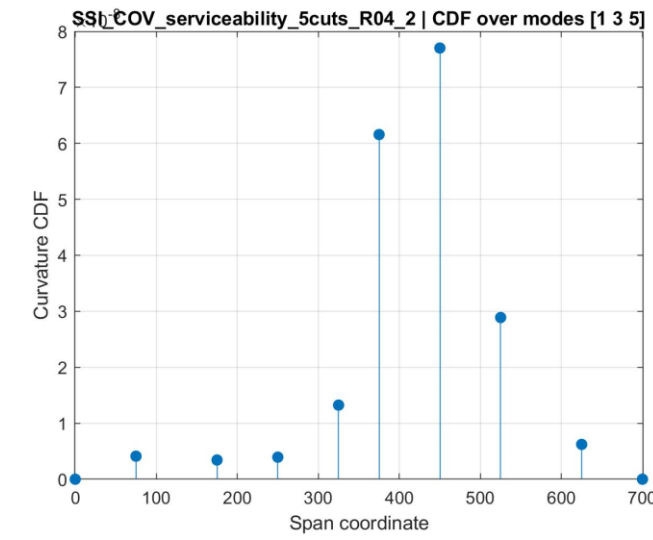
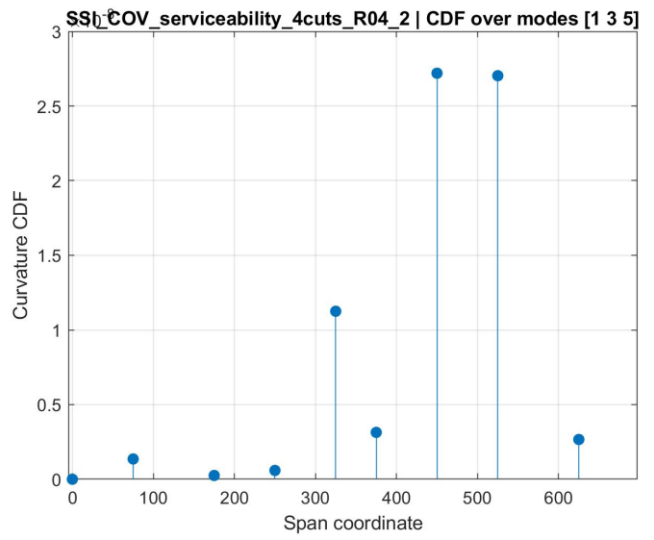
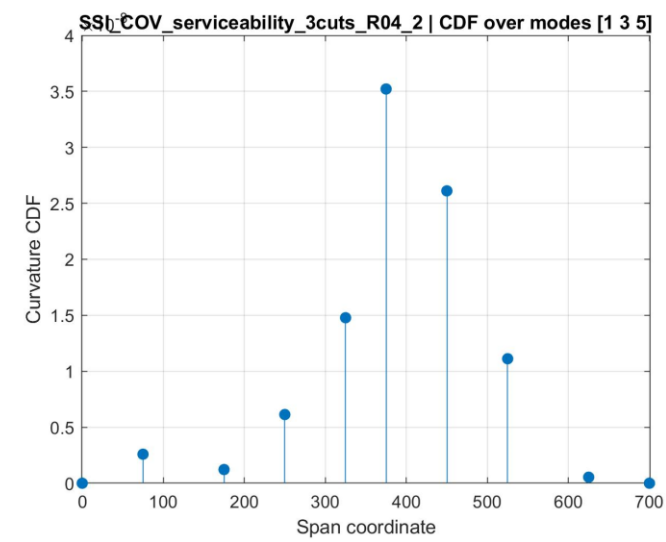
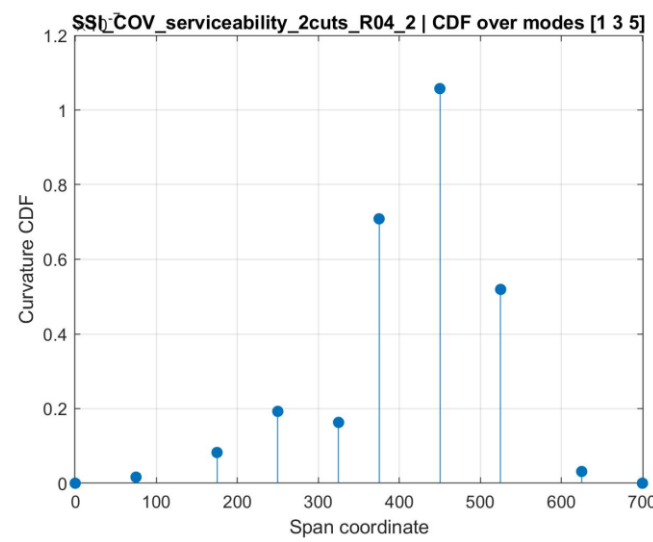
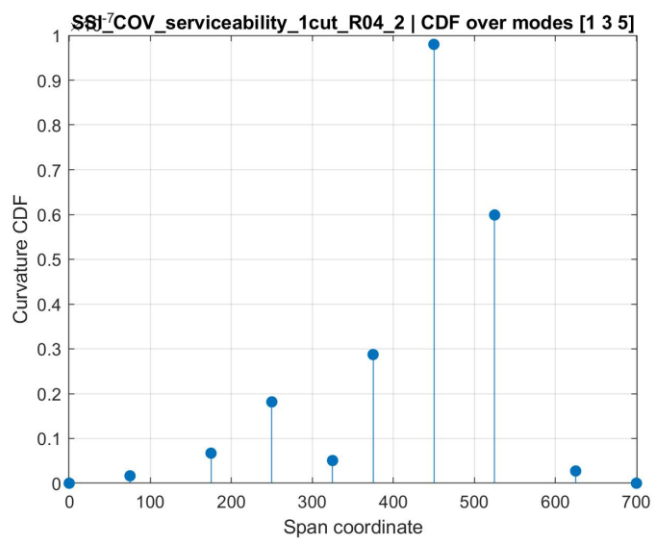
$L/3 = 466 \text{ cm}$



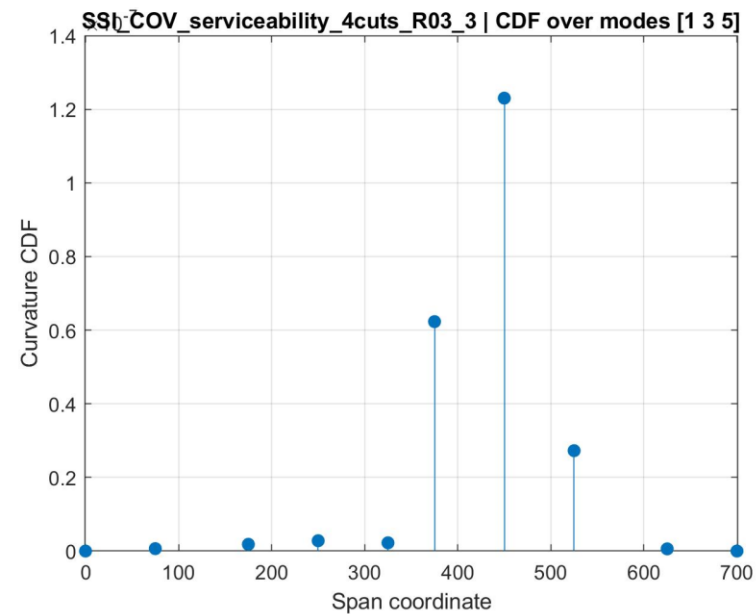
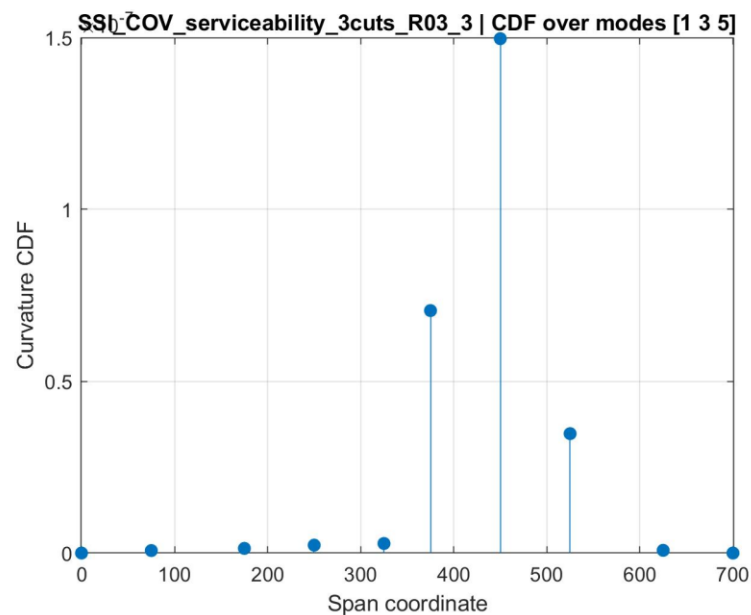
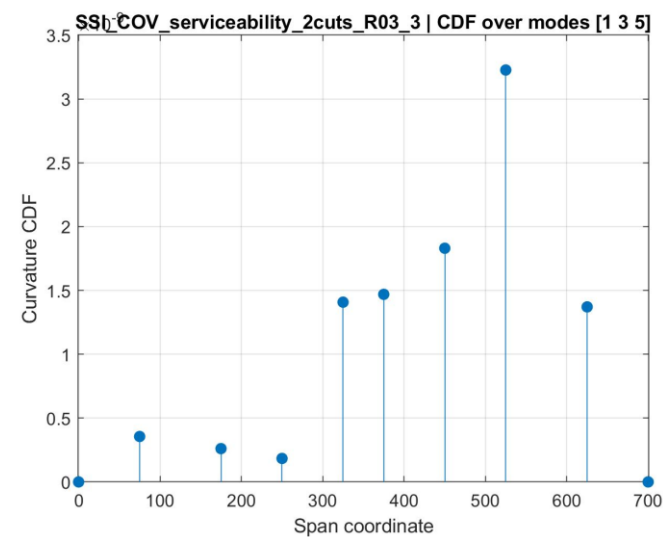
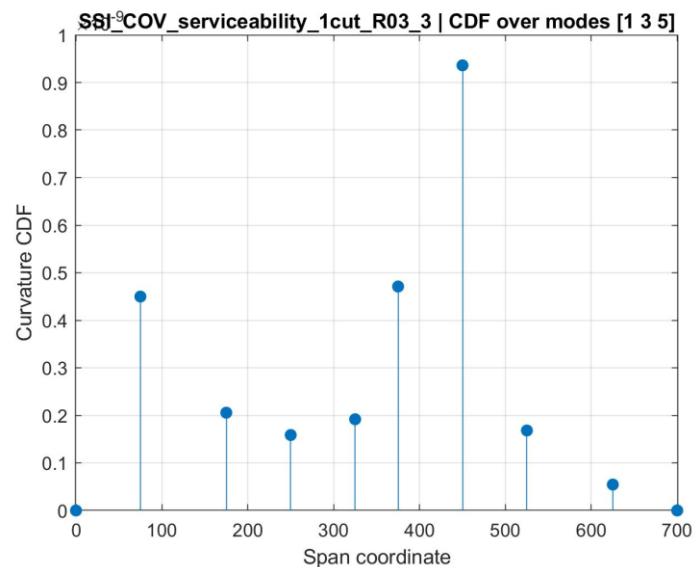
Bonded beam – Damage at L/2: Curvature CDF for bending modes



Bonded beam – Damage at L/3: Curvature CDF for bending modes

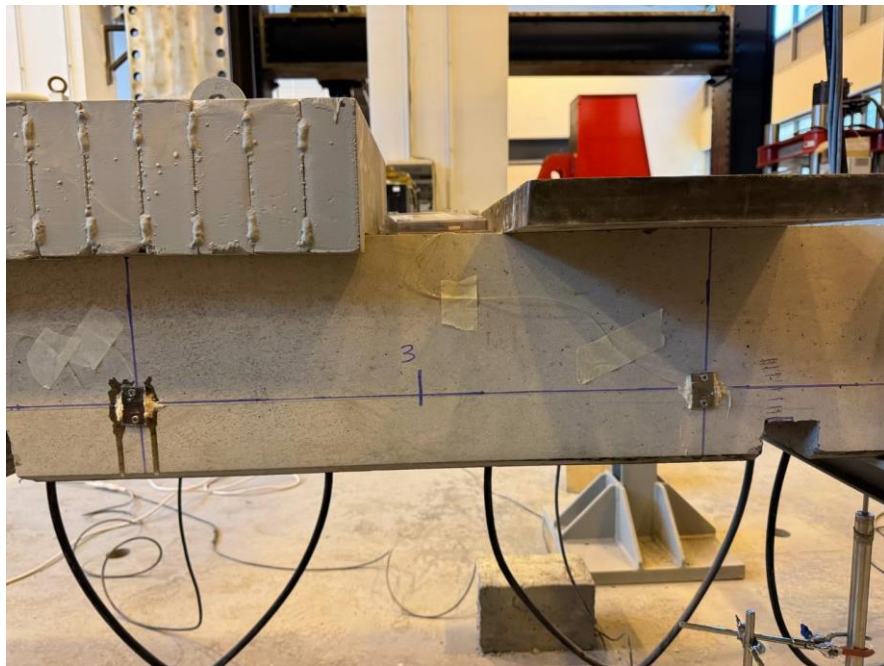
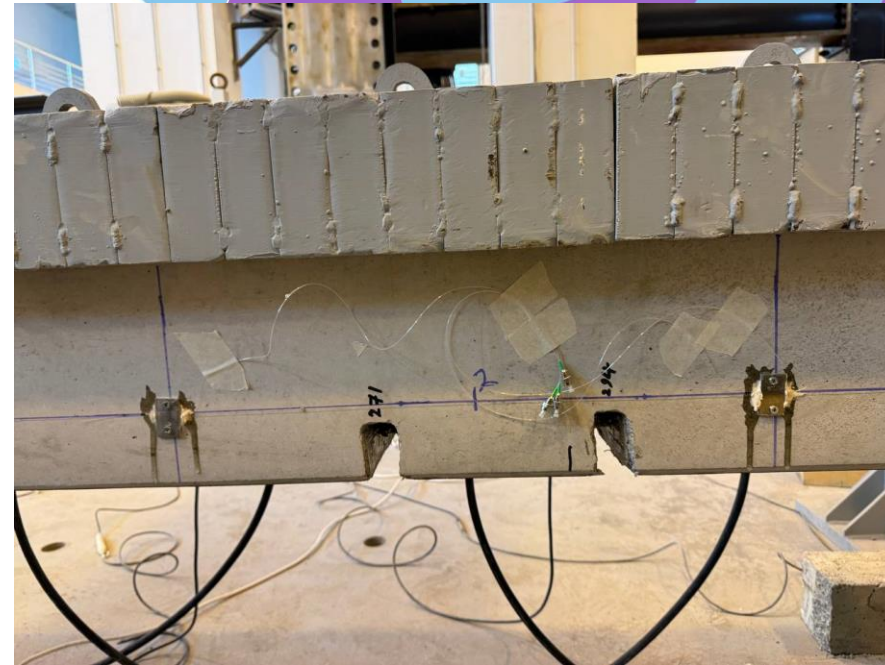
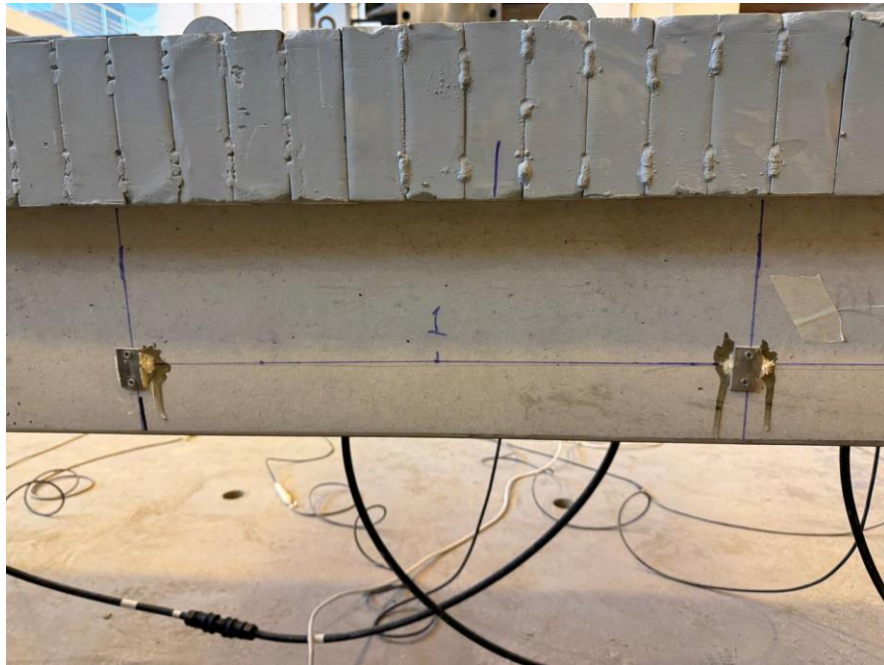


Bonded beam – Damage at L/4: Curvature CDF for bending modes



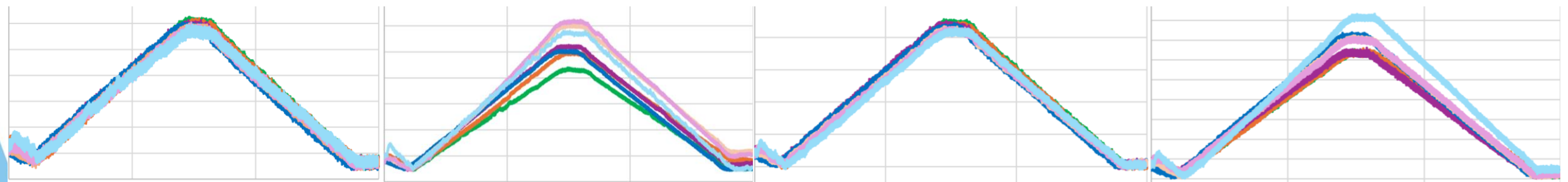
R04-3 : Damages in three inspection window







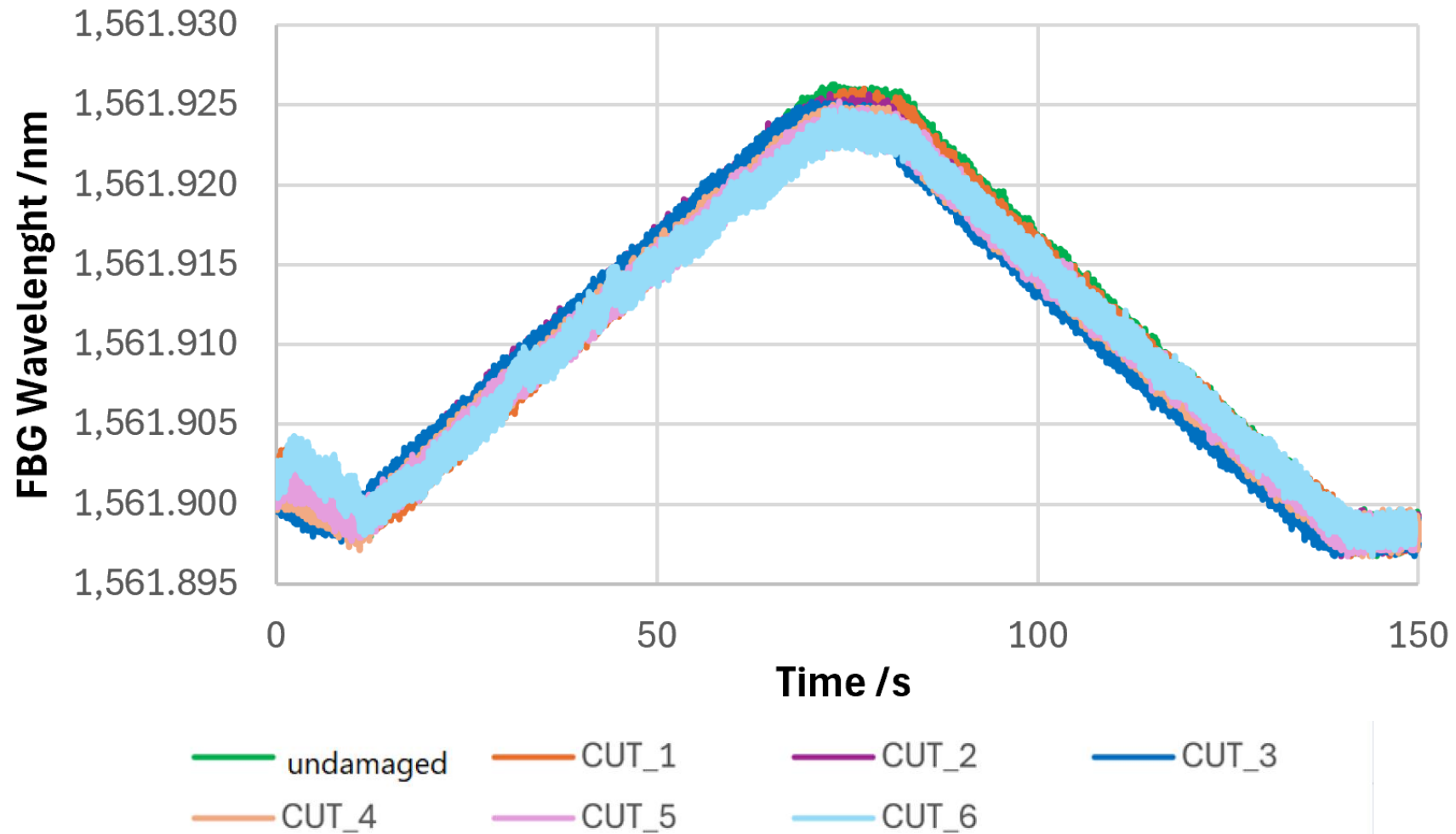
Serviceability _ loading unloading15kN _All zones



— undamaged	— CUT_1	— CUT_2	— CUT_3
— CUT_4	— CUT_5	— CUT_6	

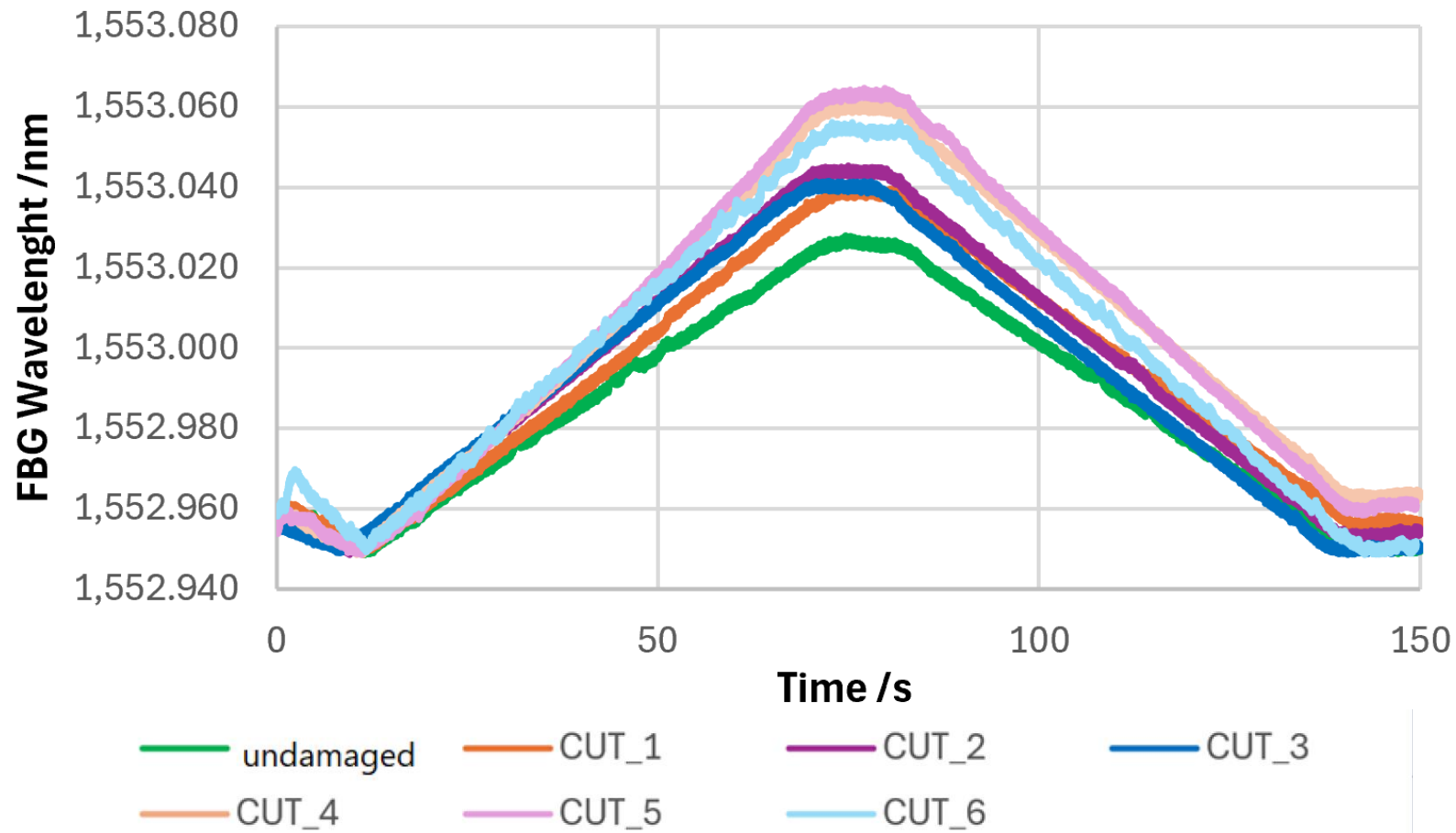
Serviceability _ loading unloading15kN

Zone 1



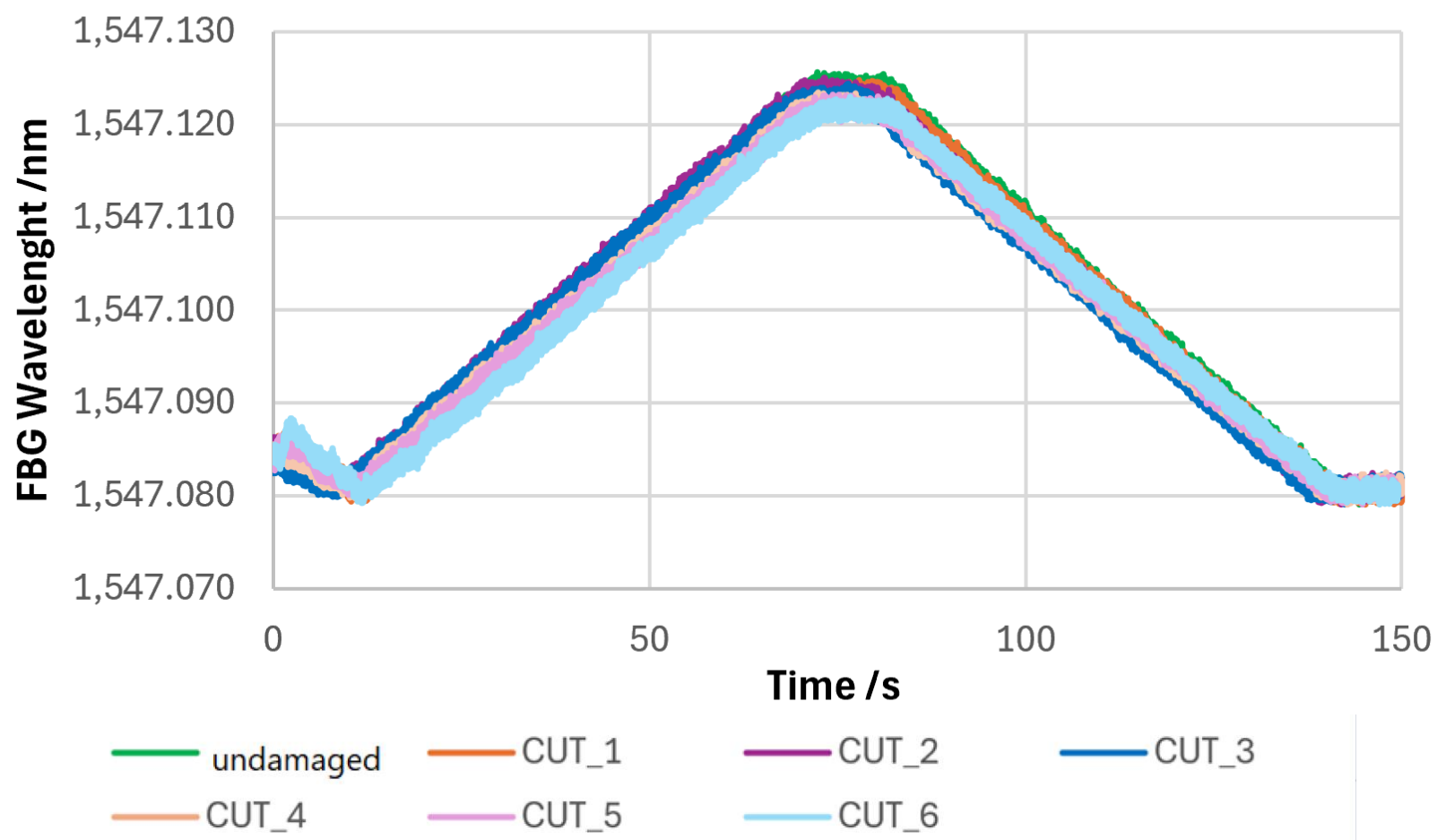
Serviceability _ loading unloading15kN

Zone 2



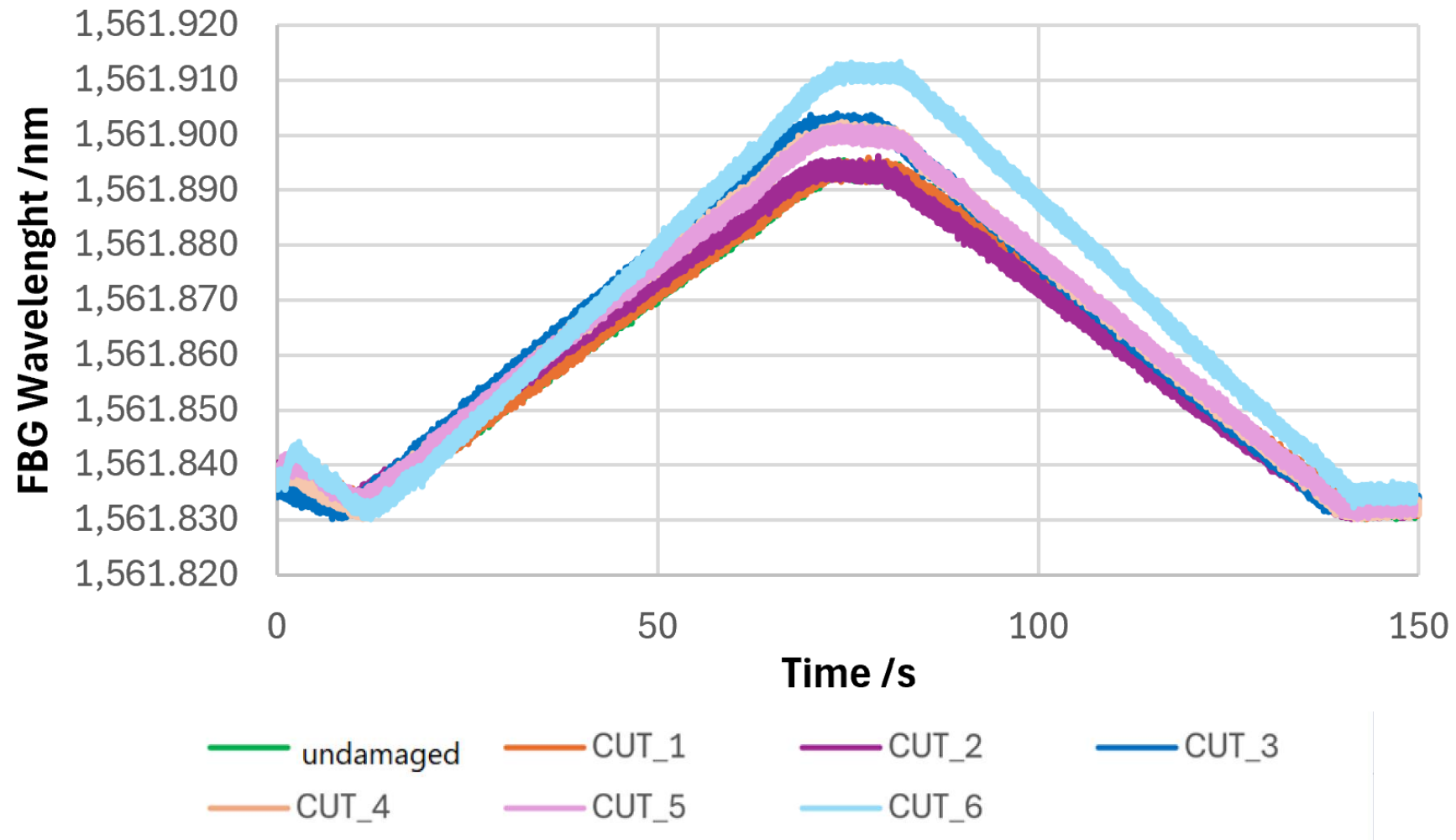
Serviceability _ loading unloading15kN

Zone 3



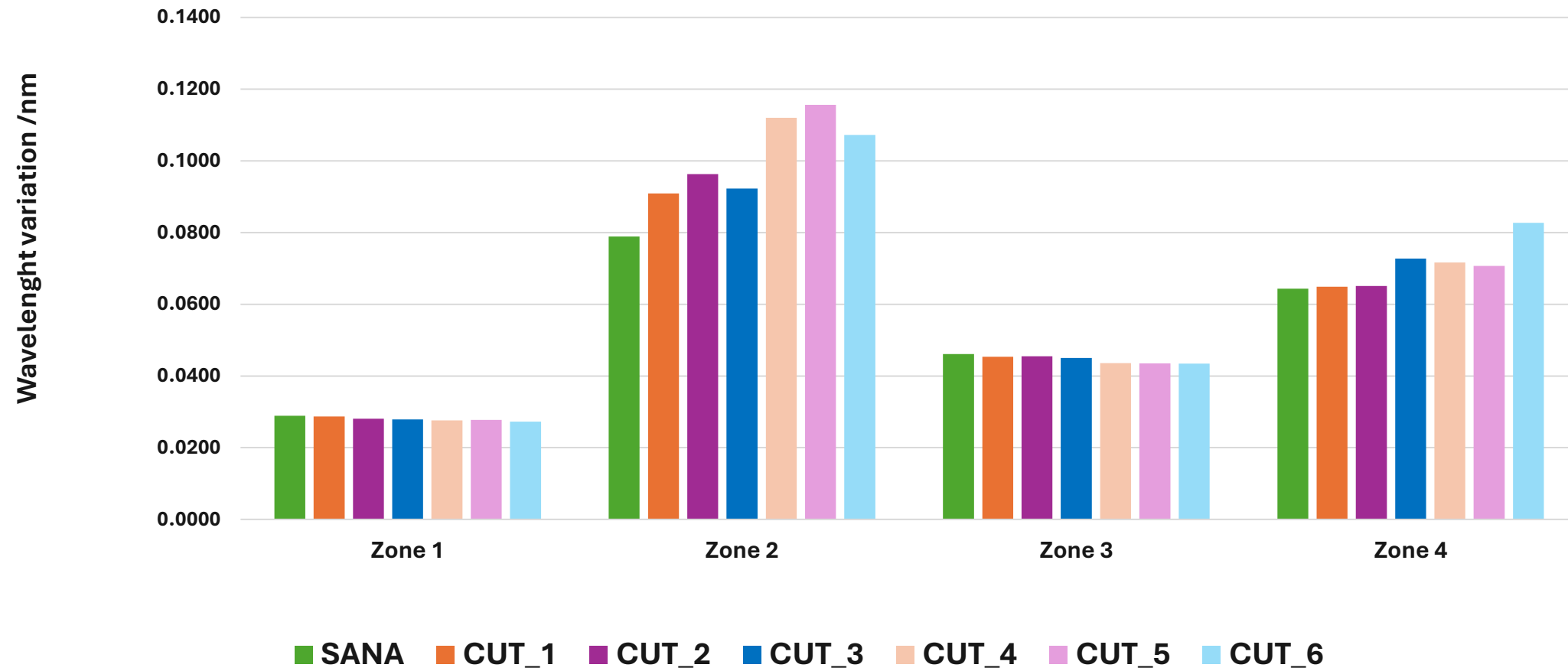
Serviceability _ loading unloading15kN

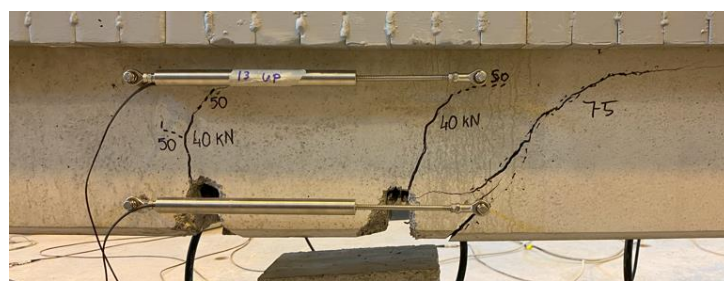
Zone 4



Serviceability _ loading 15kN

Delta Wavelenght





Università
degli Studi di
Messina

DIPARTIMENTO DI INGEGNERIA

THANK YOU FOR YOUR KIND ATTENTION

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dario.dedomenico@unime.it